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Robot Localization for FIRST Robotics

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Robot Localization for FIRST Robotics

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A Major Qualifying Project Report

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Abstract

The goal of this project is to develop a camera-based system that can determine the (x,y) coordinates of one or more robots during FIRST Robotics Competition game play and transmit this information to the robots. The intent of the system is to introduce an interesting new dynamic to the competition for both the autonomous and user guided parts of play. To accomplish this, robots are fitted with custom matrix LED beacons. Two to six cameras may then capture images of the field while a FPGA embedded system at each camera performs image processing to identify the beacons. This information is sent to a master computer which combines the six images to reconstruct robot coordinates. The effort included simulating camera imaging, designing and developing a beacon system, implementing interfaces and image processing algorithms on an FPGA, meshing image data from multiple sources, and deploying a functional prototype.
Executive Summary

This project involved the design and construction of a location tracking system for robots during FIRST Robotics Competitions (FRC). FRC is a large annual international competition between high school teams organized by FIRST, in an effort to expose high school students to engineering challenges. In preparation for the competition, students have 6 weeks to design and build a robot to play a game developed by FIRST. Each year, the game is changed to present a new challenge for contestants. In the past, robots have performed tasks in an arena such as throwing basketballs into hoops, hanging objects in a certain order, and throwing Frisbees.

We designed and implemented a low-cost camera-based robot localization system to add a new dynamic to FRC. This system sends the robots their locations in real-time, which allows teams to enhance the capabilities of their robot, and allows FIRST to provide new, more complicated challenges. For instance, teams could experiment with more precise control when launching objects towards goals by knowing not only what direction the goal is in, but how far away the goal is. It also opens the door to having longer autonomous game-play periods with more advanced path planning requirements.

To realize this dynamic, our robot localization system uses custom programmable LED beacons that provide unique patterns for each of the robots for visual identification. The beacons were made using a colored LED matrix connected to a microcontroller that controls the matrix pattern via a custom PCB that we designed. Each robot in the arena is fitted with a beacon and multiple cameras placed in specific locations around the arena are capable of viewing the beacons. The camera images are processed to identify the robots in the image, and each robot's position is calculated from these images.
Each of the six cameras on the edges of the arena is connected to an FPGA development board via a custom PCB that we also designed for this project to form a camera/FPGA vision subsystem. Each camera sends image frames to the FPGA, where the frames are processed, stored, and interpreted in order to locate and identify the beacons within the image. Then, the information about each detected beacon from each of the vision subsystems is sent to a central PC where the physical coordinate reconstruction is performed.

To provide reliable information to the PC, the FPGAs perform a number of critical operations on the incoming frames. First, the data format of the incoming frames is converted from YUV to RGB using a color space converter. Next, a color filter stage filters and normalizes the colors in the image for enhanced performance during the identification process. Next, the modified frame is stored in RAM. The FPGA logic was designed in Verilog using Xilinx design tools. A soft-core Microblaze microprocessor was also generated inside the FPGA that searches through the RAM to find pixels that had passed the filtering stage, and then interprets them to find the centers of each beacon. Beacons that are found are then compared to the expected signature of each unique pattern in order to determine which beacon corresponds to which robot.

Finally the location of the center of each beacon within the image plane is sent to the central PC with an associated unique ID. Using algorithms we implemented, the pixel coordinates of each received beacon are mapped to locations in the arena. The calculated coordinates are transmitted wirelessly to the robots during the competition.

The system we designed has been successfully tested and implemented using a single beacon, FPGA/camera vision subsystem, and PC. The full scale tests we performed indicate that our system can calculate the location of the beacons accurately to within eight inches consistently. The system is capable of running in real time, and the final step required to deploy
the system is to duplicate the hardware and synchronize communication so there are six camera/FPGA subsystems running at once.
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Chapter 1: Introduction

The FIRST Robotics Competition (FRC) is a large international competition between high school teams. It is organized by FIRST, which stands for “For Inspiration and Recognition of Science and Technology.” This organization was founded in 1989 by Dean Kamen with the goal of increasing appreciation of science and technology and offering students opportunities to learn important skills be exposed to engineering practices. High school students are given six weeks to build a robot that weighs less than 120 pounds and can operate both autonomously and under wireless direction. These robots are given tasks to complete, and the team that completes the task most effectively wins the competition.

The games for the FRC are different every year. In 2011, the game was called “LOGOMOTION.” In this game, robots were required to pick up pieces of the FIRST logo and place them on a rack on the opposing team’s side of the arena in the same order as the logo. Once this task is completed, the robots released a miniature robot which was capable of climbing the posts within the arena. In 2012, the game was called “Rebound Rumble.” In this game, teams used robots to toss basketballs into hoops on the opposing team’s side of the arena. There were four hoops and the higher hoops awarded more points to the scorer. A typical FIRST arena environment is shown in Figure 1 below.
FIRST creates interesting new challenges for the competition each year. As such, they are always open to new forms of improving their competitions. For example, they used technology from the Xbox KINECT in their competition in 2012. In the course of this project we designed a system that can be incorporated into new FRC challenges to introduce entirely new game types and provide a powerful new tool to the students involved.

The main goal of the system we designed is to provide the competing robots with their locations in real time during the competitions. Providing the robots with their precise locations in real time would allow robot teams to execute elaborate team actions, and allow individuals to make more informed decisions about their actions. The ability for robots to know their own precise coordinates can also allow FIRST to design interesting new game types that enhance the overall experience for everyone.

In order to begin defining our system, we developed a list of requirements. These requirements were based on logistical, financial, and technical considerations for FIRST. Our system aims to put as little burden on event organizers, participants, and the fans as possible, while providing useful location tracking information to teams and their robots to make the games more fun and make the learning experience better for the high school students.
The first requirement for our system is that it is capable of consistently identifying all robots individually. The data produced by our system would not be useful if it merely detected the positions of unspecified robots. Adding the ability to identify robots as individuals ensures that teams will be able to use the data we provide effectively.

In order for our tracking system to be useful, it must be accurate. To meet this requirement, we aimed for our system to be accurate to within 3 inches. However, so long as the system is relatively accurate, it will be of use to the competitors. We strove to make the system as accurate as possible while keeping the overall cost of the system low enough for FIRST to incorporate the system into their competitions.

Further, our system must not disrupt the flow of the FRC challenges. This means that our system must be assembled and initialized quickly and seamlessly before a FIRST event begins. Additionally, the system must be capable of functioning for an entire event without requiring maintenance. Finally, our system must cost a reasonable amount so that organizers can afford to utilize the system.

In our research, we determined that the most effective method for fulfilling the goals and requirements of this system utilizes cameras. Based on simulations and other design considerations, our design called for the use of six cameras. These cameras were placed around the arena as can be seen in Figure 2 and Figure 3 below.
Since the robots in FIRST competitions are quite variable in size, height, and shape, we decided the best way to uniquely identify the robots consistently was to design a beacon that is capable of displaying multiple unique patterns and place it on the robots. When the system processes the images, it searches for this beacon and associates the particular beacon pattern with a robot.
After we process the images from each camera, we combine the data from all of the cameras to locate the robots in the arena. This is done using similar concepts to stereo-vision, but with up to six cameras being integrated into the system. Using six camera stereo-vision also allows the system to see robots that have traveled near obstacles that may obscure the ability of a particular camera to see them.

The next chapter describes the background work that guided the design process. Chapter 3 will discuss the system design, and Chapter 4 will describe implementations we created to facilitate system development. Chapter 5 will explain the details of our implementation, and Chapter 6 will show the system tests we performed and their results. Finally in Chapter 7 we will show the results of our tests and the conclusions we drew from these results.
Chapter 2: Background

This chapter describes the background work we carried out for the project. It includes becoming familiar with the FIRST arena environment, investigating camera-based tracking methods, investigating the geometry involved with mapping pixels onto a surface, and investigating image processing algorithms.

2.1: The FIRST Robotics Arena

Each year the participants of the FIRST Robotics competition are given the layout of the arena in mid-January. This information is provided when FIRST holds a kickoff event where the teams are provided the rules of the game as well as the layout of the arena for the upcoming tournament. The one thing that is consistent is that the arena is always 27 feet wide by 54 feet long. The arena itself will have different aspects to it each year depending on the objective of the game. For the 2013 game the arena consists of slots to toss a disk in as well as pyramids to climb. A layout of this arena can be seen in Figure 4 below.

Figure 4: FIRST Arena for 2013 [2]
In previous years the field has had components such as ramps, racks and different pieces of equipment that can either aid the teams or add more complexities to give the robots a more difficult challenge.

2.2: Image Basics

Digital images can come in many forms. Some are visual, while others are produced by sonograms or radar. Some are colored, while others are black and white or grayscale. Basic grayscale digital image processing begins by assembling an array of values, each representing a pixel from the image. Often, these pixels are simply assigned a number within an 8-bit range, which provides 256 unique values. These values correspond to the intensity of the light in the pixel. As seen in Figure 5, the higher intensities correspond to whiter shades of grayscale [3].

![Grayscale Pixel Intensity](image)

Figure 5: Grayscale Pixel Intensity [3]

Other images can include color values, often with thousands or millions of distinct colors available.

2.3: Tracking Methods for Robot Detection and Identification

While researching camera vision-based tracking methods, we found some interesting methods that had been used for localization by others. Our design decisions were informed with some of the concepts below, including using thresholds to isolate objects within an image and
using color pattern recognition. We also explored overhead camera use but found it to be overly burdensome for FIRST.

2.3.1: Elevated Cameras with Color Detection and Thresholding

A paper called "Tracking a Robot Using Overhead Cameras for RoboCup SPL League" by Jarupat Jisarojito discussed a project using elevated cameras to determine the real world coordinates of a robot on a playing field [4]. Two cameras were placed just to the side of the field in an elevated position such that each camera covered slightly more than half of the field. An example of the setup can be seen in Figure 6 below. In the actual setup, cameras were placed directly over the goals and angled such that the maximum amount of the field is covered.

![Figure 6: The Field with Cameras][4]

As each frame is captured, the image is compared to a previously determined background image. The two images are subtracted to remove the background and the resulting image is converted to grayscale. At this point, a threshold is applied that converts the image to black and white where black pixels represent pixels that are the same as the background and white pixels represent pixels that are significantly different from the background. In addition to the
background subtraction, the areas outside of the arena are ignored. This ensures that moving objects, such as people, that are outside of the play area are not falsely detected as robots. Figure 7 below shows the empty arena (left), the arena with a robot (middle) and the image after the threshold and masking are applied (right) [4].

![Figure 7: Using Thresholds to Convert Colored Images to Black And White][4]

Each robot is outfitted with color patches in order to determine the location and orientation. These colors are reapplied after the thresholding and masking are complete. That image is converted to the original hues, the patches are detected and the centroid of the blue region (at the center of the head) is determined. This region is mapped to a grid where each grid location can be mapped to a real world coordinate. In this application, each grid represented an area with dimensions of 400mm by 500mm. Using this system, the average error between the actual position of the robot and the system determined position was on the order of 100mm. However, differences of up to 440 mm were also observed [4].

Some problems were found in this system. Some areas of the field had strong lighting and therefore reflected off of the head of the robot and affected the observed color negatively. This could be overcome by using an active system that generates its own light instead of relying on reflected light. Additionally, this method could allow for different colors to be used and therefore robots could be uniquely identified whereas this system does not allow for specific identification of robots. Further, this system does not have enough accuracy for our purposes. Worst case
errors in the position of the robot were 17.6 inches. This issue could be resolved by using more than two cameras. This would improve accuracy and would allow for redundancy in the case where one robot occludes another from view [4].

2.3.2: Colored Pattern Recognition

A paper entitled “Robottracker – A System for Tracking Multiple Robots in Real Time” by Alex Sirota discussed the use of a program to track multiple robots in an arena in real time [5]. This application was aimed towards miniature robotic Lego cars which would move around the arena. The basis for the tracking was based upon the RBG color space. Each Lego racer was fitted with what was described as a “hat” on the top of it. This “hat” is a series of circles in a target display as shown in the Figure 8 below.

![Figure 8: An RGB Color Pattern](image)

Using specific circle patterns consisting of red, blue and green colored rings that can have anywhere from 3 rings for a possibility of 21 different object to track. This can be a single ring a double ring or a triple ring target. Each ring is designated by a code with red representing the number 1, green representing the number 2 and blue representing the number 3. In the case of this coding Figure 8 above would have RGB code (123) [5].

Next using threshold values in the program the users can eliminate noise and other components such as contrast to give the camera optimal viewing of the target. The analysis of the targets follows a simple block diagram as seen below in Figure 9 in which the system detects
the targets, then analyzes the region and their colors, then detects the ID related to the color code [5].

![Diagram](image)

Figure 9: Moving From Colored Image to Identification Step [5]

The modules for this system are designed using C++ and use a variety of programs to detect and analyze the targets. Frames are captured in BMP, PPM or AVI format and then analyzed to find any hat patterns located in the image. An analyzed frame from the camera can be seen in Figure 10 below.

![Image](image)

Figure 10: An Image Frame Showing Separate Targets Being Recognized [5]

### 2.4: Number of Cameras

One paper we studied examined many of the kind of systems previously described and drew some conclusions. The paper concluded that using multiple cameras allows for a larger
visible range and allows for the use of redundancy to reduce errors. Figure 11 below shows a scene involving the use of multiple cameras to track objects. Camera $C_2$ is dedicated to the yellow and green areas. Camera $C_1$ is dedicated to the blue and green areas. The two of them overlap in the green area, where redundancy can be utilized, but data sharing must be incorporated. Overlapping is complicated to implement, but offers substantial benefits to accuracy [6].

![Figure 11: Multiple Cameras Tracking Objects](image)

## 2.5: Mapping Pixels Onto the Arena

Before moving forward with camera selection, we desired to create an imaging model that would allow us to test various camera parameters and select the proper components to meet our requirements. In order to make an imaging model, we had to understand the mathematical properties describing perspective distortion and mapping image plane coordinates onto a scene. The preliminary exploration we performed is shown below.
2.5.1: From ends of the arena

In Figure 12 below, an example image is presented. The dashed lines represent the borders of square pixels as part of an image plane. The thick red lines represent the borders of a hypothetical FIRST Robotics arena. The camera view is angled downward onto the arena from the center of one end of the arena.

As we can see, there is some perspective distortion. The far end of the arena appears to be more narrow than it really is, and the arena appears not to be as long from end to end as it really is. In calculating the positions of various robots, this distortion must be accounted for, or else the desired 3-inch accuracy of our tracking system would be unattainable.

In Figure 13, we can see a side cross-sectional view of the scene presented in this example. The length of the space between the camera lens and the end of the arena is $L$. The height at which the camera lens is place is $H$. The camera viewing angle is $\theta$. Each dashed line represents the border of a pixel, similar to the ones shown in the previous image. $L_n$ is the length of the captured space in the highest pixel of the camera module. $L_{n-1}$ is the length of the captured...
space of the second-highest pixel of the camera module. Notice that $L_{n-1}$ is shorter than $L_n$. This clearly shows how the perspective distortion is manifested in this hypothetical application. As the pixels on in the camera module move from the bottom of the image to the top, the amount of distance represented per pixel increases steadily.

![Cross Section of the Scene](image)

Figure 13: Cross Section of the Scene

There are a number of potential ways to minimize this error. The use of multiple cameras as shown below is one way, as shown in Figure 14 below. In this example, both cameras would monitor the entire arena and then average their interpretations of the position of a robot to reconcile their disagreement. In this method, using more cameras enhances the accuracy of the system. However, this also increases the cost of the system.
Another way to address this error is shown in Figure 15. The two cameras are placed in the same locations as before, but they each have their own dedicated space on the arena and they are lower from the floor. This allows the cameras to utilize all of their pixels for just one half of the arena, reducing the error from the perspective distortion. The space between the pixel boundaries is not large enough for the error to become large. However, there is still an error. Using this method also presents new challenges for setting up the system. If the two cameras overlap in their tracking space, something would have to address the potential that a robot would be identified by both cameras.
2.5.2: Using an Overhead Camera

Another way to reduce the effects of perspective distortion is to use an overhead camera. This configuration has a number of advantages and a number of disadvantages. One advantage is the reduced effects of perspective distortion.

To better understand the effects of the perspective distortion with a vertical camera placement, a cross-sectional view is presented in Figure 16. We can see that as before, the number of pixels along either the X or Y axis of the pixilated image is divided evenly among the degrees of the viewing angle \( \theta \). Since the camera is placed over the center of the arena, the distortion varies symmetrically on either side of the arena.

One can see that if the camera is raised in elevation, the increase in perspective distortion as one travels from the center of the arena outward would be reduced, but the space that each pixel covers would be increased. Raising the camera further is a way to reduce this distortion, but a camera with a significantly higher resolution would be needed to maintain accuracy for the tracking system.
While some problems are solved, new ones arise. The camera would have to be held somehow above the arena. This means it would have to be suspended from the ceiling or held up by a structure. This would drastically increase the cost of the system and the burden it places on FIRST organizers.

To solve this problem, multiple cameras would have to be placed above the arena so that they could be suspended from lower heights. However, they would still need to be suspended and more cameras cost more money and present more logistical challenges.

Figure 16: Cross Section of the Scene with One Overhead Camera

2.5.3: Quantifying Perspective Distortion

In order to make a real system that tracks real robots, this distortion must be corrected on-site in some sort of algorithm. One way to do this is to assign each pixel on the camera a corresponding set of (x, y) coordinates with respect to the arena floor. Once the pixel showing the target is identified, it would be compared with the pre-determined association between pixel location and arena location.
To understand this association, we must first understand that the camera viewing angles in the X and Y directions and the resolution are important. At the heart of this mathematical relationship are two parameters of interest. These are the number of degrees per pixel in the X direction, and the number of degrees per pixel in the Y direction.

These parameters are of interest because, as can be seen in Figure 17, we can see that the pathway to each pixel boundary where it meets the arena floor is related to the radius of a circle.

![Figure 17: Aid for Calculation of Space Covered Per Pixel](image)

**The Math**

- $x$ = number of pixels in the x direction in the camera
- $\theta$ = Camera viewing angle in the x direction
- $g = \theta/x$ = Degrees per pixel in the x direction
H = r1 = height of the camera
r2 = distance from camera lens to Point 2 in the x direction
L1 = length of the area between Point 1 and the first pixel boundary
L2 = length of the area between the first pixel boundary and the second pixel boundary
P = Pixels from the center of the image

We start with just one triangle, formed between Point 1, the camera lens, and the first pixel boundary.

\[ L_1 = H \times \tan(g) \quad (2.1) \]

The next triangle is formed between Point 1, the camera lens, and the second pixel boundary.

\[ L_2 = H \times \tan(2g) \quad (2.2) \]

Continuing further, the general relationship is

\[ L_N = H \times \tan(P \times g) \quad (2.3) \]

This relationship can be used to show the position of any pixel in an image, mapped to the FIRST arena. To form the coordinates \((x, y)\), the equations for the \(Y\) direction are the same, but with different parameters, which are given by the camera.

**Notes**

Later, the above calculations were found to only be useful when mapping the pixels along one-dimensional lines on the arena space. Further research was done to find a more robust mathematical relationship between the image plane and arena surface, and it is discussed in Chapter 4.3.
2.6: Image Processing Algorithm

Since our system requires the ability to examine an image and identify specific features, we researched existing algorithms that could be used for this purpose. The most useful algorithm was found in a paper titled FPGA Implementation of a Single Pass Real-Time Blob Analysis Using Run Length Encoding [7]. This algorithm begins by assuming that background pixels and object pixels have already been distinguished from one another. Figure 18 is the example given in the paper showing the difference between the original image and the filtered image.

With the image filtered, the algorithm scans each line from left to right. When an object pixel is identified, the adjacent pixels that have already been scanned are examined. If all of these pixels are background pixels, a new label is assigned to that pixel. If any of these belongs to an object, the same label is assigned to the pixel in question. Figure 19 demonstrates this process.
If multiple pixels are identified on the same line, the start and end pixel locations for each run of consecutive pixels are noted. At the end of each line, the runs for the current line are compared to the runs of the previous line to determine if there is any overlap. If overlap occurs, the run for the current line is given the same label as the run that it overlaps. If no overlap occurs, the run is given a new label. This operation can be seen in Figure 20.

When the algorithm encounters a run that overlaps with two or more runs on previous line it merges the two previous runs into a single run. When this happens, the information relating to the first run is combined with that of the second such that the final run accurately represents the entire object as it has been scanned. An example where merging is required can be seen in Figure 21 below.
After every line has been scanned, the centroid is determined using the following equations [7].

\[ x = \frac{1}{A} \sum u \]  
\[ y = \frac{1}{A} \sum v \]

(2.4)  
(2.5)

A is the area of the box surrounding the object, \( u \) is the horizontal location of each pixel in the blob, and \( v \) is the vertical location of pixel in the blob. After this calculation, the true center of each object has been determined.
Chapter 3: System Design

From our background research, several issues were found that should be addressed. Our system needs to be capable of tracking robots on an entire 27x54 foot field, that can have various obstacles and ramps that can block sightlines and change the heights of robots. Also, since each robot is independently controlled, each of the 6 robots playing the game should have a unique visual ID that can be identified, independent of the robot’s design. Once images are captured, a system must be developed to analyze the images to find the unique IDs. Then the perspective distortion of the camera must be corrected, which allows accurate reconstruction of robot locations.

The system that we designed to accomplish the goal of this project operates in four major stages. The first stage of the system involves utilizing an array of LEDs to generate a specific pattern of colors. The second stage is the image acquisition stage where images from the camera are captured and stored. The third stage is the image processing stage where key data is extracted from the images. The fourth and final stage is the reconstruction stage where data from multiple cameras are combined to determine the locations of the robots.

Figure 22 below shows the overall hierarchy for the full scale system. This system uses six cameras placed around the arena. Each has its own FPGA embedded system to process the images and send the results to the central PC. Once the data from the six cameras has been received by the central PC, the locations of all of the robots are reconstructed and provided to FIRST for distribution to the teams.
One of the most crucial aspects of our project was the selection of our camera. We needed to choose a camera that would be able to see all aspects of the arena while being able to handle the requirements needed to accurately take pictures and communicate with our FPGA. The quality of our camera has a direct impact on the accuracy of our system as a whole. As a result, we performed extensive research in order to choose the best possible option for our system.

3.1.1: Camera Resolution

In order to make sure we were purchasing a camera which could handle the needs of our system, we created the imaging simulator described in section 4.3 to test the accuracy of potential cameras. The simulator included user defined parameters covering the different aspects
of a camera specification such as the field of view of the lens and the camera resolution. After running the simulator, an image was produced that showed how effectively that camera would be able to locate robots within the arena. Examples of these images can be seen Figure 23 and Figure 24 below. In Figure 23, the camera was placed at the bottom left corner of the arena and angled down at a 45 degree angle. In Figure 24, the camera was placed at the center of one of the edges of the arena and was again angled down at a 45 degree angle. In both of these figures, green indicates that the error at that location was less than 3 inches, yellow indicates that the error was less than 5 inches, red indicates that the error was less than 7 inches, and white indicates that the camera could not see that part of the arena.

![Heat Map of Accuracy from a Corner](image)

Figure 23: Heat Map of Accuracy from a Corner
3.1.2: Camera Interface

Our process in searching for the right camera took us across many different pieces of equipment. Originally we looked into security cameras and focused specifically on field of view and resolution without paying attention to the interface with the rest of the system or the cost for each camera. This meant that we were leaning towards high end models of cameras which cost in the range of $800 to $1500 each. After further investigation, it became clear that we had to focus on other aspects of the cameras because the models we were leaning towards had outputs that would be burdensome as part of an image processing system. We chose to use a camera that outputs its data serially in a raw image format instead of a camera that outputs its data in compressed format via USB. In order for us to use a USB camera, we would need a computer with a USB interface and the required software to interpret the data for each camera. This is not a cost-effective implementation so we decided to use a camera with raw data transmitted in an uncompressed format.

3.1.3: Camera Specifications

Once we decided on a camera that provided uncompressed data, we came to the conclusion that we would need a camera that provided data in either RGB or YUV format. Also
on our list of specifications was a horizontal viewing angle of at least 95 degrees as well as an 86.5 degree vertical viewing angle to allow a 5 degree tolerance in either direction. These angles would allow us to cover the field completely with enough overlap between the separate cameras to ensure that the system would function with a high degree of accuracy. In looking at the camera modules it became clear that we would be able to look for specifications such as resolution and data output and leave the viewing angle issue for our choice of lens.

After performing research we decided to use the 24C1.3XDIG shown below, which is a camera module produced by Videology. The camera can be seen in Figure 25 below.

![24C1.3XDIG Camera Module](image)

**Figure 25: 24C1.3XDIG Camera Module [8]**

We arrived at this piece of equipment after looking through many other cameras. This camera outputs a digital 8 bit YUV output and has a 1.3 Megapixel sensor that can output images up to a resolution of 1280 x 1024. This camera is also flexible in that it can use a variety of lenses that fit into a CS, M12 or pinhole lens mount. Finally, it is significantly less expensive than the other high end cameras we looked at since this module would end up costing $200.
3.2: LED Beacon

An important part of our project was the use of LEDs to identify and locate the robots. This beacon was designed with the intent that it would be placed on top of the robots during the competition to serve as a target for locating and identifying the robots within the arena. The beacons have been designed in such a way that up to twelve beacons can be in the arena simultaneously and that each beacon will have a unique pattern associated with it. The matrix used for the beacon can be seen in Figure 26 below.

![Figure 26: LED Matrix with PCB Controller and MSP430](image)

3.3: Image Acquisition and Processing

In order to specify the hardware for the Pre-Processing stage, we first determined the requirements of this stage. We determined that this stage must be able to operate at a speed that is faster than the clock rate of the camera, and that it must be capable of a pipelined data flow in order to avoid data loss. The data must be converted from YUV to RGB, passed through a filter, and stored in RAM without losing or corrupting a single piece of data.
With an entire frame accessible in RAM, the image processing stage begins. This stage uses a soft-core microprocessor to process the image. The intent of this stage is to find the center of each beacon and identify which robot the beacon belongs to. This is done by first using a modified version of the Run-length encoding algorithm described in Chapter 2. This new algorithm finds all adjacent pixels that are of the same color and groups them together. After this initial scan is complete, the groups are examined with respect to each other. If two groups are determined to be adjacent to each other, they are interpreted as being part of the same beacon and an identifier is assigned to the center of that group based on the colors of the pixels in each group. The block diagram for these two stages can be seen in Figure 27 below.

![Image Acquisition and Image Processing Block Diagram](Figure 27: Image Acquisition and Image Processing Block Diagram)

In order to implement these two stages, we chose to use an FPGA as it is capable of performing the required logical operations at a higher speed can be configured to implement a pipelined data flow. After choosing to use an FPGA as the platform to implement our image processing stage, we chose a specific FPGA to use. We chose to use a Spartan 6 FPGA on a Nexys3 development board. This board was chosen because of the FPGA and the peripherals
such as the RAM as well as UART and VGA display ports it contains. This FPGA is capable of operating at a speed significantly higher than the camera we chose and is large enough that it is able to easily support our system design. The RAM peripheral on this board is necessary for storing an image so that the entire image can be processed at the same time. With all of these capabilities, the Spartan 6 FPGA on a Nexys3 development board was the best choice for developing our Image Processing stage.

3.4: Beacon Location Reconstruction

Once each camera has finished processing a frame, it transmits the pixel coordinates of the center of each beacon along with its identifier to a central computer. The final stage reconciles data from multiple cameras in order to reconstruct the real world coordinates of the beacons. The program that runs the user interface with the PC and performs the coordinate reconstruction was made to be portable so any PC running Windows can run the program.
Chapter 4: Modules for Testing

4.1: Camera Model

Since many of the Verilog modules we developed relied on receiving data from the camera, we developed a model of the camera. This model was designed in such a way that it produced the same signals as the camera. These signals included 8 bits of image data, a signal indicating when a horizontal line had ended, a signal indicating when a frame ended, and the 54 MHz clock that the camera provides. With this model successfully implemented, we were able to test our digital logic models in simulation. By simulating these modules, we significantly decreased the amount of time required to debug each system. This is because simulations provide significantly more visibility of all of the signals in a module than testing on a physical FPGA would.

4.2: VGA Display

In order to facilitate our testing, we designed a module that was capable of reading image data from RAM and displaying it on a VGA display. This module has two main components. The first component generates the timing signals required to communicate with the display. This is done by using a 25 MHz clock which increments two counters. These two counters drive synchronization signals which set the monitor to display an image at 640X480 resolution. The second component utilizes a FIFO to ensure that color data is always available and accurate. This is done by continuously writing pixel data from RAM until the FIFO is full. While data is being written in, data is simultaneously read out to drive the VGA display. By doing this, the display will always have pixel data ready when it is needed.
After implementing the VGA Display module, a testbench was created in order to verify that data was available to send to the display at the proper times. The result of this test can be seen in Figure 28 below. This figure particularly demonstrates that data is passed into the system 64 bits at a time and sent to the monitor 8 bits at a time. Additionally, the signal that indicates that the FIFO cannot hold more data is shown.

![Figure 28: VGA Display Testbench](image)

### 4.3: Imaging Model

Since our project is based on using images to find object locations, it was very important to develop an understanding for how three-dimensional locations are projected onto a two-dimensional image plane. This was done by developing a model for the camera. Initially a simple model was developed, but it was found to be too limited, and did not accurately represent the camera. This motivated the development and implementation of a more complex imaging model.
The initial model developed attempted to treat horizontal and vertical displacement in the image as functions of single angles. Distance left or right from the center of the image was assumed to be a function of a single angle because the object imaged was to the left or right of an imaginary plane determined by the yaw angle of the camera as shown in Figure 29, and distance up or down was assumed to be because the object was above or below a plane determined by the pitch angle of the camera. This created an easy model to calculate, but we noticed it did not properly simulate images of objects when implemented. For instance, Figure 29 shows a red and green object being imaged by a camera located at the bottom left corner of the setup. Since the objects are on the same line of sight from the camera, our initial model created the image shown in Figure 30.

Figure 29: Overhead View of Objects on Field Being Viewed By A Camera
We then measured out Figure 29 in the lab, and took an image with an actual camera, which is shown in Figure 31 below. Clearly, this figure demonstrates that the green object should be closer to the image center than the red one, so our simple camera model did not accurately represent how a camera maps real world locations to images. Since it wasn’t capable of accurately simulating a mapping from real-world locations to image locations, it would have been unsuitable to try inverting the process and determining real-world locations from an image. The figure below shows how the setup in Figure 31 would actually be seen by a camera.
To address the limitations of the initial model, the more complex pin-hole camera model was implemented and used. This model uses rotation matrices to perform frame transformations between field coordinates and camera coordinates, like those seen in Figure 32.

This rotation is accomplished by multiplying 3 3x3 matrices that encode the roll, pitch, and yaw of the camera with respect to the field’s coordinate system. For example, a roll of the camera, which is a rotation around the axis perpendicular to the image plane, is represented as:

$$R_{\text{roll}}(\theta) = \begin{bmatrix} \cos(\theta) & 0 & \sin(\theta) \\ 0 & 1 & 0 \\ -\sin(\theta) & 0 & \cos(\theta) \end{bmatrix}$$ (4.1)

This is useful because multiplying this matrix by any 3 dimensional position vector will properly rotate the vector into a new frame described by the rotation, for example, substituting 90 degrees for \(\theta\), and multiplying by a vector \(\langle 1,0,0 \rangle\) will result in:

$$R_{\text{roll}}(\theta) \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ -1 \end{bmatrix}$$ (4.2)
This indicates that a 90 degree roll is a transformation around the y-axis of the field. A single simple rotation matrix like \( R_{\text{roll}} \) is a rotation around a single axis. By combining 3 of them, a full 3 axis rotation can be created. Our camera model uses a full rotation matrix of:

\[
R = R_{\text{roll}}(\alpha)R_{\text{pitch}}(\beta)R_{\text{yaw}}(\gamma)
\]

\[
= \begin{bmatrix}
\cos(\alpha) & 0 & \sin(\alpha) \\
0 & 1 & 0 \\
-\sin(\alpha) & 0 & \cos(\alpha)
\end{bmatrix} \begin{bmatrix}
1 & 0 & 0 \\
0 & \cos(\beta) & \sin(\beta) \\
0 & -\sin(\beta) & \cos(\beta)
\end{bmatrix} \begin{bmatrix}
\cos(\gamma) & -\sin(\gamma) & 0 \\
\sin(\gamma) & \cos(\gamma) & 0 \\
0 & 0 & 1
\end{bmatrix}
\]

(4.3)

This allows us to specify the direction of any camera using 3 angles \( \alpha, \beta, \) and \( \gamma \), and any vector \( <x,y,z> \) in field coordinates can then be rotated into an equivalent vector \( <u,v,w> \) in camera coordinates as in Figure 33.

![Figure 33: Rotation of Q in frame (x,y,z) to Q' in frame (u,v,w)](image)

Once this frame transformation is complete, the vector in \( <u,v,w> \) is converted to homogeneous coordinates, by dividing the vector by \( w \), this creates a vector,

\[
Q'_{\text{homogeneous}} = \begin{bmatrix} u \\ v \\ w \\ 1 \end{bmatrix}.
\]

Since the \( w \) axis is perpendicular to the image plane of the camera, this vector ends on the image plane of the pinhole camera. Then \( Q'_{\text{homogeneous}} \) can be pixelized based on the field of view and resolution of the camera, which allows us to accurately model how an object appears in a camera image.
In summary, by measuring the distance between the camera and a point in field coordinates \((x,y,z)\), and multiplying that vector by \(R\) to rotate the vector into camera coordinates, then converting it to homogenous camera coordinates and pixelizing the result, we could accurately map a real-world camera pose and object location to an actual image. This mapping accounted for the impact of all 6 degrees of the camera's pose in generating the horizontal and vertical image locations of an object, rather than just 4. This allowed us to simulate much more accurate representations of how our camera would view different objects. Figure 34 shows an accurate simulation of the image of the scene in Figure 29, using the pin-hole camera model described. The black line indicates the center of the image for reference. Note that the green block is closer to the center line than the red block.

![Accurately Simulated Image](image)

**Figure 34: Accurate Simulation of setup in Figure 29**
This imaging model was heavily used throughout project development. It helped us determine how camera and lens parameters such as resolution and field of view impacted our field coverage, which helped us develop our design specifications. It also helped quantify beacon size and pattern resolution limitations. Finally, it was used directly to map images back to 3 dimensional locations once the central PC received the image data from the FPGA.
Chapter 5: System Implementation

With testing modules successfully implemented, we were able to implement and test our individual modules. This chapter describes the requirements, implementation process, and tests performed for each module we developed.

5.1: Tracking Beacon

Our tracking beacon had to be designed and constructed in a manner that was efficient and compatible with our camera system. This section describes how we designed and implemented our beacon to meet this requirement.

5.1.1: Requirements

The requirements for our beacon were very straightforward. The first was that it had to be clearly visible to our camera and able to be powered by the robots in the competition. Another requirement was that there had to be the ability to display multiple patterns in order to uniquely identify multiple robots within the arena. The final requirement of the tracking beacon was that it had to be simple enough that people who worked the FIRST competition with no knowledge of the system would be able to work our beacon design. Patterns for the beacon can be selected simply by pushing a button.

5.1.2: Design Choices and Considerations

The beacon design evolved from many different ideas. We first came up a set of 3 LEDs in a triangle for our beacon consisting of red, green or blue. This was because the front LED could be used to help identify which robot was which due to the position of the 2 rear LEDs. This allowed us to track up to 6 possible robots but lacked the ability to expand that number should FIRST decide to add more robots to a playing field. Also in implementing the LEDs we
decided to use RGB tri-colored LEDs because they were easily identifiable, as well as being easier to use because of the simplicity in changing the color of the LED when needed for beacon patterns. The idea behind this method was to use trigonometry to determine a reference point’s location as seen in Figure 35 below.

![Figure 35: Original Beacon Layout](image)

Once we determined that this beacon concept did not provide enough different patterns to identify the robots uniquely, we decided to move onto a different beacon design as seen in Figure 36 below. This design was chosen because it could be easily detected by a camera due to the area it occupies.

![Figure 36: LED Beacon Design](image)
However, after receiving and testing the LEDs in lab, we came to the conclusion that this design was inefficient because it would require more space to implement and this would make our design being more intrusive to the competitors.

With size consideration and efficiency in mind, we went researching new ways to implement a tracking Beacon. After doing research we came across an LED Matrix and decided that this would be the best solution. The matrix we used to implement our design can be seen in Figure 37 below.

![LED Matrix](image)

**Figure 37: LED Matrix for Beacon Design**

### 5.1.3: Tracking Beacon Design

The beacon design for our LED matrix went through many different stages. In order to implement set of unique pattern designs, we configured our matrix to have four different sectors which would each occupy a 4 by 4 quadrant of the LED matrix. An example layout of our beacon can be seen in Figure 38 below.
The pattern design for tracking has 4 quadrants that get illuminated to represent RGB colors. Because of our cameras ability to differentiate between colors we can combine 2 colors such as red and green or red and blue to minimize the space of our beacon and still ensure that each quadrant can be detected. We have designed the patterns such that they are easily identifiable for the image processing stage of our system. In total we have 12 unique color patterns as described in the table below to allow FIRST the ability to increase the number of robots in the arena while still ensuring that our system will be able to accurately track the beacons. In a typical FRC game, six robots are used and all of these robots can be tracked by our system.
Table 1: Identification Patterns

<table>
<thead>
<tr>
<th>Pattern Colors by Quadrant</th>
<th>ID Number</th>
</tr>
</thead>
<tbody>
<tr>
<td>RRRY</td>
<td>1</td>
</tr>
<tr>
<td>RRRG</td>
<td>2</td>
</tr>
<tr>
<td>RRRP</td>
<td>3</td>
</tr>
<tr>
<td>YYYYR</td>
<td>4</td>
</tr>
<tr>
<td>YYYYG</td>
<td>5</td>
</tr>
<tr>
<td>YYYYP</td>
<td>6</td>
</tr>
<tr>
<td>GGGR</td>
<td>7</td>
</tr>
<tr>
<td>GGGY</td>
<td>8</td>
</tr>
<tr>
<td>GGGP</td>
<td>9</td>
</tr>
<tr>
<td>PPPR</td>
<td>10</td>
</tr>
<tr>
<td>PPHY</td>
<td>11</td>
</tr>
<tr>
<td>PPPG</td>
<td>12</td>
</tr>
</tbody>
</table>

The reason we chose to use three quadrants next to each other as the same color with the final quadrant being a different color is because it allowed our image processing system to easily distinguish between different patterns.

5.1.4: LED Matrix Controller

In order to control what tracking pattern was seen on the LED matrix we needed to design a PCB that would control the voltage input to each quadrant. After looking into the matrix’s pinout it became apparent that we would need to multiplex the matrix in order to display the correct color in each of the four quadrants.

At first we discussed using a shift register for the output controller in order to be able to control each LED separately. Soon it became clear that using shift registers would overcomplicate our design because we only needed to control individual quadrants instead of individual LEDs. This led us to believe that a simple MSP430 microcontroller would be the best option to use for multiplexing purposes because of its simplicity. Using this microcontroller we could tie off the rows and columns into groups using h-bridges. This allowed us to use only 8
I/O lines. These lines are for Rows 1-4 and 5-8, Red Columns 1-4 and 5-8, Green Columns 1-4 and 5-8, as well as Blue Columns 1-4 and 5-8 as seen in Figure 39 below.

![Diagram of Row/Column Grouping](image)

**Figure 39: Layout of Row/Column Grouping**

This method of grouping simplified our design because each group was connected to an output of a quadruple half-h driver. We decided to use the half–h drivers as can be seen in Appendix B because of their ability to work with the current requirements of the LED matrix as well as the microcontroller. To implement this design we used two of these drivers to control specific quadrants as needed to display the correct pattern.

**5.1.5: Beacon Implementation**

With the requirements and design specifications discussed in the previous section, we designed our PCB for implementation. The prefabrication layout of our LED Matrix Controller PCB can be seen in Figure 40 below.
Figure 40: Prefabricated LED Matrix Controller PCB

After all of our components were acquired and the PCB was fabricated, we populated the board for testing. The final assembled LED Matrix Controller can be seen in Figure 41 below.
Finally attaching the matrix and Launchpad to the PCB we were able to test our design to verify its functionality. Our assembled Beacon can be seen in Figure 42.
5.1.6: Testing

After beginning testing with the LED PCB, it became apparent that the beacon was not behaving as predicted. The patterns that were being displayed can be seen in Figure 43 below.
Upon testing the connections between the matrix and the PCB it was discovered that some of the lines to one of the headers were reversed. The Figure 44 shows what the original header orientation was.

![Figure 44: Former Board Layout](image)

Based upon the pinout of the LED matrix the header should have been positioned as follows in Figure 45.

![Figure 45: Necessary Board Layout](image)

In order to correct the PCB error we created a new basic breakout board to reverse the orientation of the headers to ensure they connected to the right signals. Finally once this was done we retested the Matrix and all twelve of the beacon patterns displayed correctly. Figure 46 below shows the Matrix displaying pattern 3.
5.2: Camera PCB

In order to communicate with the FPGA our camera needed a custom breakout board that connected the signals from the camera to a connector on the Nexys3 development board. This was necessary because the connector for our camera was not available on the Nexys3 board. Our custom circuit board was designed to provide the necessary connections between the camera and the Nexys3. The board needed to incorporate two connectors; a 30-pin Molex mating connector for the camera, and a 68-pin VHDCI connector to connect with the Nexys3 board. Connecting to the VHDCI connector was preferable to the other connections available on the Nexys3 because it is designed for high-speed data transfers and is designed for high speed data. The appropriate connections to the camera were made in accordance with the Digilent Nexys3 functional descriptions of the various VHDCI connector signals when designing the custom board.

5.2.1: PCB Design

Figure 47 below shows the board design before it was sent for fabrication. The camera plugs in within the bounds of the dark blue lines. It has mounting holes on two corners, designed
to correspond with the mounting holes on the camera module itself. Also, some screws and nuts were selected to mount the camera to the board during operation so it did not fall off when tilted upside down.

There are four surface mount circuit elements that were added. Three are capacitors, one is a resistor. Capacitor C1 and resistor R1 serve as the shield for the VHDCI connector. They are used in a low pass configuration in order to prevent voltage spikes in the signals. Capacitors C2 and C3 are decoupling capacitors that filter out noise from the power supply to the camera.

The four holes on the corners were added to the board to allow for standoffs to be added so the board would rest at the same height as the Nexys3 and also protect the solder connections from wear. There are 12 labeled test points on the board to use during testing and debugging of the board, camera, and FPGA logic. Figure 48 below shows the fabricated PCB and Figure 49 shows the fabricated PCB connected to the Nexys3 development board.
We used the test points to initially confirm that all connections had properly been made between the camera and the FPGA. The test points also played a critical role in verifying the
functionality of the camera and in development of the I²C communication with the camera because debugging that communication was made easier by observing the communications on an oscilloscope.

5.3: I²C Interface

The Videology 24C1.3xDIG camera we used has user-selectable settings for all sorts of camera features. These include resolution, gain control, contrast, shutter speed, as well as several others. In order to adjust these for optimal settings, an I²C interface was created using a Micoblaze soft-core processor which is generated inside the FPGA.

There are eleven configurable registers with settings for this camera. The one that is of most immediate interest to us was register 0 which contains the settings for the frame rate, gain mode, and resolution. The settings available for resolution and frame rate are in the Figure 50 below:

![Figure 50: Resolution and Frame Rate Chart](image)

In Figure 51, all the available settings configured in register 0 are shown, bit by bit. For our testing purposes, VGA (640X480) resolution has to be used. This is because SXGA (1280X1024) resolution requires a 108 MHz pixel clock for use with a VGA display, but the fastest we could read data from the SRAM on the Nexys3 board is 80 MHz.
To set the camera to VGA resolution, bits 15:14 needed to be 01 in binary as can be seen in Figure 51. Also, we wanted to change the mains frequency from the default of 50 Hz to 60 Hz which is more easily compatible with standard 640X480@60Hz for the monitor. To achieve these settings, we needed to write 0x40C3 to register 0.
The oscilloscope image in Figure 52 above shows an entire sequence to read the data in register 0 from the camera. The clock is entirely driven by the master, which is our FPGA, except when the slave (the camera) is stretching the clock.

Figure 53 above shows the results of the read action displayed on the seven segment displays on the Nexys3 board. For comprehensive reading and writing, a simple user interface
was implemented to guide the user through the short command entry process. For instance, if a user wants to read from register 0, they simply set all the slider switches to low, press the right button, and then press the down button to execute the command. The LEDs are used to show the user the status of the entry user interface.

Next, 0x40C3 is written to the camera, as shown in Figure 54 above. The process is a little simpler and shorter than a read, since the camera does not have to be re-addressed.

Figure 54: Writing 0x40c3 to Register 0
To confirm that 0x40C3 was received, the register is read again. The camera confirms that the register was what we wanted. The sequence can be seen in Figure 55 above and the seven segment display confirms it to the user as shown in Figure 56 below.
5.4: Camera Interface

The camera we used for our system provides data 8 bits at a time in UYVY format as can be seen in Figure 57 below.

Since our design requires the data to be in RGB format for processing, we needed to implement a module that packaged multiple 8-bit words into single 32-bit words, macropixels. These macropixels are passed on to the other modules as they become available. We decided that the simplest way to implement this packaging mechanism was to use a FIFO. The FIFO takes in 8-bit words at every positive edge of the 54 MHz clock provided by the camera and produces 32-bit words at the positive edge of an 80 MHz clock, which is used by the rest of the system, if the YUV to RGB conversion module is ready for data. This FIFO serves the purpose of packaging the data for further use and performing the clock domain crossing that moves to the faster clock domain of the main system. Figure 58 below shows the block diagram for this module. This block diagram shows 8 bit data from the camera passing through the FIFO and being output as a 32 bit macropixel.
5.5: Beacon Filter

The main purpose of the Beacon Filter module is to filter out image data that is not part of one of the LED Beacons or calibration markers. This is done in two phases. First the image data is converted from the YUV color space to the RGB color space. A filter is then applied that removes data that does not fit the profile of an LED Beacon or a Calibration Marker. This filter also normalizes all data that matches the profile so that further image processing can be performed in a simpler manner.

5.5.1: Color Space Converter

The first step in performing the filtering is to convert from the YUV color space to the RGB color space. This conversion is done by first breaking the macropixel from the camera interface into two pixels. A macropixel contains 4 words of data that correspond to data for the two pixels in the following manner: \( U_{0/1} Y_0 V_{0/1} Y_1 \). This data is broken up to form two pixels as follows: \( Y_0 U_{0/1} V_{0/1} \) and \( Y_1 U_{0/1} V_{0/1} \). Once these pixels have been assembled, the math required
to convert from the YUV color space to the RGB color space is applied. This is done by applying the following equations.

\[
Y = R \times 0.299 + G \times 0.587 + B \times 0.114
\]  
(5.1)

\[
U = (R - Y) \times 0.877283
\]  
(5.2)

\[
V = (B - Y) \times 0.492111
\]  
(5.3)

The submodule that applies this math has been pipelined such that the computations take 7 clock cycles to complete.

In addition to the conversion submodule we used, we designed custom digital logic that served to control the data flow within this module. In order to signal that the data on the output is valid, a signal is given to the submodule that is passed through the pipeline with the data that is being converted. This signal is driven high when valid data is applied at the input and a signal from the output of the pipeline is driven high when valid data is available at the output.

The data flow for this module can be seen in the block diagram in Figure 59 below. Raw image data comes from the Camera Interface module. Each macropixel is multiplexed such that individual pixels are sent to the YUV to RGB Converter so that each pixel is converted in the proper order. When the data has been converted, it is compressed so that it requires less space in RAM and can be easily used to drive the colors on a VGA display. Finally, the data is packaged in a FIFO so that 64 bits of data can be written to RAM at the same time.
When the implementation of this submodule was completed, a testbench was created that applies simulated data from the camera and demonstrates that the data is assembled properly for use in other modules. The results of this test can be seen in Figure 60 below. Of note is this test bench is that data is applied on the camera_data input. This data is converted and the results of this conversion can be seen on the processed_data_in wire. It is then passed to the compressor which shrinks the data down to 8 bits per pixel and writes the compressed data into the FIFO. Finally, the 64 bits of packaged data can be seen properly assembled on the dout line.
5.5.2: Color Filter

With the image data in RGB format, the first portion of the image processing can be executed. This stage filters out image data that is not part of an LED Beacon or a Calibration Marker. This is done by comparing the Red, Green, and Blue values of each pixel to predetermined threshold values. Six values are used; three that check if a color is above a minimum value and three that check if a color is below a maximum value. For example, in order for a pixel to pass through the filter with the color yellow, it would need to have Red and Green values above the minimum thresholds for those colors and a Blue value below the maximum threshold. This ensures that the only colors that get through the filter are those that are purely one color or another. Additionally, this stage filters out most data that is not relevant to the LED Beacons or the Calibration Markers. This stage has the limitation that bright sources of light that are located in the arena will not necessarily be removed since they have the proper profile.

The block diagram for the completed Beacon Filter module can be seen in Figure 61 below. This block diagram has replaced the simple data compressor block with the more complex Color Filter block described in this section.
This stage was tested using the VGA Display module. The results of these tests can be seen in Figure 62 and Figure 63 below. Figure 62 shows an image that was taken by our system with the color filtering disabled. Figure 63 shows the same scene with filtering enabled. In both of these figures, the white crosshair was used to identify the center of the image and was not actually perceived by the camera. All of the data that was not part of the calibration markers or LED Beacon was removed and the important colors had their values normalized successfully.
The RAM Interface module was designed in order to facilitate use of the onboard RAM. The interface has three main purposes; configure the RAM with the appropriate settings, perform a write operation, and perform a read operation. The first step in developing the interface was to determine how to configure the RAM. Once this was completed, the read and write operations were developed.

5.6.1: RAM Configuration

When the configuration settings for the RAM were being chosen, the biggest consideration was the speed at which writes could be performed. Our limitation was that data came in from the camera 8 bits at a time at a rate of 54 MHz. Since the RAM has an upper bank and lower bank, each of which holds 8 bits per address, we were able to write 16 bits at a time. Therefore, we needed to be able to perform writes at an average rate of 27 MHz. We initially considered using the asynchronous access mode of the RAM, but we quickly discovered that this would operate at 1 write per 70 ns which is on the order of 14 MHz. We then found that synchronous burst mode write operations could be performed much faster. This is because
multiple writes can be performed in quick succession as long as the addresses are consecutive. We chose to operate the RAM at its maximum clock rate of 80 MHz and in 4 word burst mode. At this speed, the RAM requires 7 clock cycles to prepare a write, then performs a 4 writes over the next 4 clock cycles. Therefore, in a worst case scenario, 4 writes are performed in 11 clock cycles which averages to be a rate of 29 MHz which is above our requirement.

Once these settings were chosen, we developed the method for programming these settings into the RAM. This is done by performing a write to the Bus Configuration Register (BCR). A write to the BCR is done by driving the RAM input signals as seen in Figure 64 from the MT45W8MW16BGX datasheet [10].

![Figure 64: BCR Write Operation][10]

The key signals to drive for the BCR write operation are the address lines, CRE, ADV#, CE#, and WE#. CRE is driven high to indicate that a configuration register access is being performed. ADV# and CE# are both driven low to indicate that the chip has been enabled and that the data on the address lines is valid. WE# is held high when ADV# and CE# are first driven.
low, but is driven low when the write is actually performed. Finally, the address lines contain the settings to write into the BCR. The data on these lines is given by the following table.

<table>
<thead>
<tr>
<th>Addr</th>
<th>Value</th>
<th>Register</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>[22:19]</td>
<td>000</td>
<td>Reserved</td>
<td>Set to 0</td>
</tr>
<tr>
<td>[19:18]</td>
<td>10</td>
<td>Register Select</td>
<td>10 for BCR</td>
</tr>
<tr>
<td>[17:16]</td>
<td>00</td>
<td>Reserved</td>
<td>Set to 0</td>
</tr>
<tr>
<td>[15]</td>
<td>0</td>
<td>Operating Mode</td>
<td>Synchronous Burst Mode</td>
</tr>
<tr>
<td>[14]</td>
<td>1</td>
<td>Initial Access Latency</td>
<td>Fixed</td>
</tr>
<tr>
<td>[10]</td>
<td>0</td>
<td>WAIT Polarity</td>
<td>Active Low</td>
</tr>
<tr>
<td>[9]</td>
<td>0</td>
<td>Reserved</td>
<td>Set to 0</td>
</tr>
<tr>
<td>[8]</td>
<td>0</td>
<td>Wait Configuration</td>
<td>Asserted during delay</td>
</tr>
<tr>
<td>[7]</td>
<td>0</td>
<td>Reserved</td>
<td>Set to 0</td>
</tr>
<tr>
<td>[6]</td>
<td>0</td>
<td>Reserved</td>
<td>Set to 0</td>
</tr>
<tr>
<td>[5:4]</td>
<td>01</td>
<td>Drive Strength</td>
<td>1/2 (Default)</td>
</tr>
<tr>
<td>[3]</td>
<td>1</td>
<td>Burst Wrap</td>
<td>Burst no wrap (default)</td>
</tr>
<tr>
<td>[2:0]</td>
<td>001</td>
<td>Burst Length</td>
<td>4 Words</td>
</tr>
</tbody>
</table>

Table 2: BCR Settings

Once the BCR write operation was implemented, a testbench was created that would execute the operation on model of the RAM and verify that the operation had been implemented properly. The results of this test can be seen in Figure 65 below.

Figure 65: BCR Write Operation Testbench
5.6.2: Read and Write Operations

The proper sequences required to perform read and write operations on the RAM were determined from the RAM datasheet. The basic sequences can be seen in Figure 66 and Figure 67 below.

---

**Figure 66: Burst Mode Write [10]**

---

**Figure 67: Burst Mode Read [10]**
The major difference between the above figures and the sequences used for our implementation is that the latency for the system in the figures is 3 clock cycles where in our system the latency is 7 clock cycles. Both operations rely on the use of the address lines, ADV#, CE#, OE#, WE#, and LB#/UB#. ADV# is driven low to indicate that an operation is beginning. When this happens, CE# must also be driven low, and the data that is present on the address line is locked in. LB# and UB# are held low at all times in our design because for both reads and writes, we intend to use both banks of RAM.

In order to perform a write operation WE# must be driven low when ADV# and CE# are initially driven low. Additionally, OE# must be driven high throughout the entirety of the operation, and that WE# must be driven low at the same time as ADV# and CE#. On the first positive edge of the clock after the latency period, the data that is on the DQ line will be written to the given address. At the next positive edge of the clock, data is available from the address immediately following the given address. At the end of the operation, four address worth of data will have been read. For example, if the address given at the beginning of the operation was address 0, data from addresses 0, 1, 2, and 3 would have been provided.

A read operation differs from a write operation in that WE# must be driven high when ADV# and CE# are initially driven low. Further, OE# must be driven low during the latency period of the operation in order to indicate that a read is being performed. At the first positive edge of the clock after the latency period, valid data will be available from the given address. At the next positive edge of the clock, data is available from the address immediately following the given address. At the end of the operation, four address worth of data will have been read in the same manner as data was written for a write operation.
When the write and read operations were understood, a state machine was implemented that drove the signals as appropriate. Once the state machine was implemented, a testbench was created and the write and read operations were tested with a model of the RAM. The results of these tests can be seen in Figure 68 and Figure 69 below.

The Figure 68 demonstrates a write operation to address 0 with the following data values: 64, 8, 192, and 8. Figure 69 demonstrates a read operation on address 0 following the previous write operation. When the read operation is performed, the data values read out are: 64, 8, 192, and 8 which are identical to the values written by the write operation.

After the read and write operations were verified in simulation, the RAM interface was installed on the FPGA and another test was performed. This test repeatedly wrote four separate
values to the RAM. Figure 70 below shows one of the write operations that we intended to perform. Figure 71 below shows the contents of the RAM after our test was performed. The data appear to be out of order in the second figure. This is due to the program we used to read data from the RAM to a PC for viewing. The program reads data from the lower bank followed by the upper bank while our system writes data first to the upper bank, then to the lower bank. Since read and write operations within our system are consistent in the ordering of the banks, this is not an issue.

![Figure 70: Intended Write Operation](image1)

![Figure 71: Portion of RAM after Write Operation](image2)

5.6.3: System Interface

With the individual RAM operations successfully implemented, the last remaining portion of the RAM Interface module to be developed was the system interface. This interface was intended to provide a simple way for writes or reads to be initiated. To make the interface as simple as possible, four inputs and three outputs are utilized. The first two important inputs indicate that a write or read operation has been requested. If either of these inputs is driven high and the state machine is not performing an operation, the operation corresponding to that input
will be performed. In the event that both inputs are driven high at the same time, write operations are given priority. The third input contains the 23 bit address that the operation is intended to be performed on. This value is given to the RAM Interface instead of being sent straight to the RAM because the data on the address line must be overridden when a BCR write is performed. The RAM Interface detects when a BCR write is intended and multiplexes the signals appropriately. The final input signal is a 64 bit input that contains data that is to be written to the RAM. When a read operation is performed, the 64 bits of data are split up so that the top 16 bits of data are written to the first address; the second 16 bits are written to the second address, and so on.

The first important output signal is a signal indicating that the RAM Interface is ready to begin either a write or read operation. It can also be used to indicate that the RAM Interface is currently performing an operation. The main use for this signal is in handshaking between the RAM Interface and the module that is providing it data. The remaining two output signals are useful for read operations. One of the signals is a 64 bit line that contains the data from a four word burst read. When a read is performed, the data from the first read is stored in the top 16 bits, the data from the second read is stored in the next 16 bits and so on similar to how the data is data input is used. The final output is a signal indicating that a read has been completed and the data on the 64 bit data output is valid. This signal, similar to the ready signal, is used in handshaking between the RAM Interface and other modules that are requesting data from the RAM.

With all of these signals in place and all operations functioning properly, the RAM Interface can be used as a simple way to either write data to or read data from the RAM. Due to this simplicity, the logic required in other modules to use the RAM is significantly decreased.
5.7: Interfacing Submodules

The final step required to complete the data flow was to integrate each of the modules together. This was done by first connecting each module such that the output of one module connected to the input of the following module. Additionally, handshaking routines were developed so that data would not be lost because the sending module was ready to send without the receiving module being in a position to receive the data. With the handshaking in place, data was able to pass through the system without being lost due to miscommunication between modules and without being lost due to the system operating at too low of a speed.

Once this was accomplished, the two stages of processing that occur in the FPGA had to be reconciled. This had to be done because the RAM that was used is only capable of reading or writing at one time; it is incapable of performing both operations simultaneously. As a result of this, the system can either be in the image acquisition stage or the preprocessing stage. Since these stages require the modules to behave in different ways, a state machine was created that determines which stage is active and drives enable signals for each module as appropriate.

Finally, the system that was used to control the addressing to the RAM was developed. This system sets the address to 0 if the system has just been activated, if it has been reset, or if it is transitioning from image acquisition to image processing or vice versa. Otherwise, the address increments by 4 every time a write or read operation is detected by the RAM Interface module. This is done because the RAM only requires the address to be valid when an operation starts. Therefore, if the address is incremented immediately after an operation begins, it is highly unlikely that the address lines will not have stabilized by the time a new address is needed.

The block diagram for the integrated system can be seen in Figure 72 below. This block diagram shows the data flow through the Camera Interface, Color Conversion, and Ram
Interface modules. It also shows the complexity of the state machine, addressing, and control logic in the system.

Figure 72: Block Diagram of Integrated Modules

5.8: Image Processing

The image processing stage is the implementation that locates the center of each beacon within the image, matches each beacon with its unique ID and sends this information to the Central PC. In order to perform these tasks, the beacon identifier requires access to the image data stored in RAM by the Image Acquisition stage as well as the ability to communicate with the PC to send the information. The capability of performing the recognition and identification of the patterns within the image consistently and reliably is the central responsibility for this stage.

5.8.1: Implementation

Due to the complexity of this implementation, we decided that developing it in software was the best solution. The Spartan 6 FPGA is capable of supporting a Microblaze soft-core
microprocessor, and it is generated Xilinx ISE software. It is a 32-bit microprocessor capable of running at 100 MHz, which gives the beacon identifier plenty of capability to perform as intended.

The Image Processing algorithms begin once the Image Acquisition stage signals that it is complete the beacon identifier begins acquiring pixel values from RAM until a horizontal line worth of data is stored in a buffer. Then, the buffer is searched for colored patches. Each time a colored pixel is found, it is compared with the previous pixel. If the previous pixel is the same color as the current pixel, the current pixel is added to the patch for the previous pixel. If the previous pixel is not part of a patch, a new patch is created that starts with that pixel. Data for each patch is recorded for interpretation after the entire frame has been processed.

Once a horizontal line of pixels has been processed, the next line is acquired from RAM and the same process is performed as the previous line. However, pixels within a line are not just compared with their neighbors to the sides; they are compared with their neighbors above and below. Patches that meet the requirements we set to be considered part of the same patch are combined. This process is repeated for the entire frame.

Once all the patches are found, they are interpreted. Patches must be at least 5 pixels in size to be considered part of a beacon. This is to reduce the likelihood that a noise will pass through the filtering stage and be identified as a beacon. Patches that are adjacent to one another by five pixels in any direction but are different colors are combined into a beacon.

Algorithms are used to decrease false identifications, so that duplicates are not produced, and so that the beacons are properly matched with their unique identifier. Then, the algorithm looks at each beacon and compares the sizes of the two associated patches to determine which ID
to generate. The location of this beacon is stored along with its unique ID for transmission after each beacon has been processed.

After all beacons are identified and all non-beacon patches are discarded, the Image Processing stage enters transmit mode. In transmit mode, the matrix object information is sent to the PC for that frame, and a new frame is requested by the beacon identifier and it waits until the rest of the system is ready for more image processing to be performed on the next frame.

5.8.2: Testing

Before implementing the color patch location algorithm in the Microblaze processor, we developed it in MATLAB and tested it on some simple simulated images. The simulated image can be seen in Figure 73 and the results of this test can be seen in Figure 74.

![Figure 73: MATLAB Patch Locator Test Image](image-url)
Next, we translated the algorithm from MATLAB to C syntax and began developing the beacon identifier implementation inside the FPGA.

We decided to test the beacon identifier on a test image before moving to camera images. This allowed us to compare our results to a constant, known scenario for more efficient debugging. To make these test images, we made binary files the size of our test resolution with patches of nonzero values inserted to mimic colored pixels. These binary files were written to RAM in order to replicate how the system would work using a camera-acquired image as closely as possible.

We found that the process of reading the RAM via the Microblaze was not working properly. The first indication of a problem was when the count of beacons after processing a frame showed zero beacons despite them being present in the RAM.

Next, known data was read in smaller quantities, sent to a PC via the UART, and observed in Putty. The data was being properly read from the first location of each 4-address block, but not the subsequent three addresses within the block.

Below are screenshots of the tests we performed. We generated a new binary file to download into the RAM that contains the hex values 22 11 44 33 66 55 88 77 AA 99 in the first several addresses of RAM. We began reading addresses starting at address 0, where 0x2211 was present. The way our SRAM is configured, SRAM63_32 (the upper 32 bits of the 64-bit SRAM

```
>> Results = Blcb(xy, color)

Results =
    400    20   320    24    89
    400   300   240   137   117
      5     2     4     1     3
```

*Figure 74: Results of MATLAB Patch Locator*
read results bus) should contain those 16 bits (0x2211), followed by the next 16 bits (0x4433).
SRAM31_0 (the lower 32 bits of the 64-bit SRAM read results bus) should contain 0x66558877.
We repeated this test on the first several block addresses, and in each case, only the first address
within the block was read properly. The reason the same address is copied into all four address
spaces is because the burst was not working, so the same location was read into each address
space. An example of this issue can be seen in Figure 75 below.

![Debugging Microblaze access to RAM](image)

At that point, we could read the contents of memory properly if we only read one address
at a time. However, we wanted to be able to use the burst mode because it is a better engineering
design that allows us to read more pixels more quickly.

Through testing, we found that the RAM interface Verilog design module worked only
when the address specified for each read was provided by the Verilog design instead of the
Microblaze processor.

We found the next issue to be that the array that stores incoming pixel data was not
declared as a static variable. This was causing issues with the memory that corrupted other
variables. When we changed this, the Beacon Identifier ran to completion and identified slightly
more than the correct number of beacons. Our algorithm did not take into account beacons that
are more complicated in shape yet. To fix this, we made a function that merges beacons that share the same color and share a border. When this function was complete, the Beacon Identifier was demonstrated as identifying the correct number of beacons and all beacons were in the correct location with the correct color.

Figure 76 below describes the test that we performed at the full resolution. This image is the full scale 1280X1024 test image that we placed into the RAM.

![Figure 76: Full Scale Test Image](image)

Figure 77 below shows the output of the beacon identifier test. We used the UART communication to send out the data so that we could see it on a computer screen. As can be seen
in the image, we were identifying the appropriate number of color patches and they were centered in the correct locations and have the correct number of pixels associated with them. Note that the origin of the image is at the top left, so that larger Y values are actually lower on the image.

Figure 77: Beacon Identifier Test Output

Figure 78 below is an example of a beacon that requires merging. As each new horizontal line is scanned, two purple patches are initially detected due to the horizontal nature of our algorithms. However, further down the image we find that these two patches are actually part of the same patch. The merging function takes all of the small patches that are close enough to one another and puts them into one patch.
With our patch recognition algorithms functional, we moved on to identify beacons using the actual camera images instead of test images. Figure 79 below shows the image that appeared on the computer monitor screen after passing through the color filtering system. The second image shows the results of the test sent via UART to a computer. The results shown in Figure 80 demonstrate that the beacon was located at pixel (292, 278) with the origin located at the bottom left corner of the image. This matched what we expected from the image that was displayed on the monitor.
Similar tests were extensively performed in order to verify that the pattern identification system was fully functional.

5.9: Reconstructing Locations from Images

After image processing, the next step in the information flow is to actually resolve the (x, y) beacon locations. This is done by combining the data from the 6 cameras with knowledge of where the cameras are located.

Figure 81 above shows the goal of this part of the system. The goal is to take the known pixel coordinates, (U, V), and determine the physical location (X, Y) inside the arena space.
5.9.1: Requirements

This stage has several important requirements. It needs to resolve the camera locations quickly, account for the possibility of the beacons being at a variety of heights, and flexibly incorporate data from two to six cameras, depending on the beacon's location and the number of cameras around the field capable of identifying it.

5.9.2: Implementation

Once accurate images could be simulated from a camera pose and object location, we could move to solve for an object location based on a camera image. Initially, this reconstruction was developed assuming a height for the beacons. This allowed us to solve for a location with only one image, however, this seemed to put significant requirements on the FRC teams to mount the beacons at a specific height, and wouldn't allow our system to compensate for different terrain heights, which is a feature common in FRC games. These inflexibilities motivated a solution to use two camera images from different perspectives to first find the height of the object, and then solve for its (x, y) location as in stereo-vision. Because there are six cameras present on the field, we developed a solution that to combine the data from all 6 cameras to generate a least-squares error image reconstruction based on all the images that the object is located in.

Since a camera image provides horizontal and vertical information (a (u, v) pixel location), one image can allow us to solve for the (x, y) location of an object, provided we know the height, z, that the object is located at. This is a case of solving two equations (the mapping to u pixels, and v pixels), for two unknowns; the x and y positions of the object. However, since FRC robots vary widely in size, assuming the height of the beacon on the robot is not reasonable.
To combat this, we looked to implement a way to combine two camera images to create one 3-
dimensional location.

There were two different methods available to combine image data from two cameras to
solve for an object location. An iterative method would assume a height $z$, then calculate an $(x,
y)$ location based off of one image, then use the calculated $(x, y)$ and a different image to try to
solve for the $z$ location, and iterate until the $(x, y, z)$ location converged. Since this system needs
to quickly determine the beacon locations, this iterative method did not seem promising, so
principles of stereo-vision were employed to implement a direct method of combining the image
data. This method used the pinhole camera model developed in Chapter 4.3 to express each $(u, v)$
pixel as a 3D line, $L$, radiating from the camera's focal point. This is done by expressing the pixel
as a vector $\mathbf{v} = < u, v, 1 >$ by depixelizing it into homogeneous image plane coordinates. Then,
to reverse the homogenization, $\mathbf{v}$ is multiplied by a scalar, $S$, and multiplied by the rotation
matrix $R^{-1}$ which is the inverse of the rotation matrix used to change from $<x,y,z>$ coordinates
to $<u,v,w>$ camera coordinates, and rotates $S\mathbf{v}$ back into $<x,y,z>$ coordinates:

$$ L = R^{-1}S\mathbf{v} $$  \hspace{1cm} (5.4)

Two different cameras provide two different lines, $L_1$ and $L_2$ pointing to the same object. By
solving for the intersection of $L_1$ and $L_2$, the height of the object $z$ can be determined. Then
using either $L_1$ or $L_2$, the $x$ and $y$ components of the location can be found. This principle is
illustrated in Figure 82 below.
While this method does allow determination of the full \((x, y, z)\) position of the beacon, there will be quantization error due to the pixelization, which can be significant at long ranges, and error due to inaccurate determination of the pose of each of the cameras. These errors propagate through the system to the reconstructed locations. However, if extra data is available from other cameras, these errors can be reduced. This requires solving an over determined linear system and finding a least squares solution [11]. This was implemented by defining a linear system of the form:

\[ Ax = b \]  

(5.5)

Where \(A\) and \(b\) are column vectors with entries for each image that contains the object. Both sides of the equation are multiplied by \(A^T\), giving:

\[ A^T Ax = A^T b \]  

(5.6)
Since $A^T A$ and $A^T b$ are scalar values, solving for $x = \frac{A^T b}{A^T A}$ gives the least squares error solution for $x$, which is the best possible solution for the object’s location, given the images available. This calculation is repeated for $x$, $y$, and $z$.

5.9.3: Testing

As this system was implemented, the functionality was continually tested in simulations. Test images of objects from various perspectives were generated, and those images were used to reconstruct the beacon locations. The reconstruction was then compared to the actual location the simulator started with. This procedure was repeated with different image resolutions, camera locations, lens viewing angles, numbers of cameras, and beacon locations. The results from these simulations helped guide design decisions regarding the beacon design, camera resolution, and lens angle.

5.10: Calibration Algorithm

The accuracy of the beacon reconstruction as described above is extremely dependent on accurately knowing the pose of each camera. Since the system requires installing these cameras above the floor, it was unreasonable to assume that the cameras would be precision aligned. This motivated the development of an automated calibration routine, which uses images of objects, called calibration markers, at known locations inside the field to accurately determine the camera's pose. The calibration markers are placed temporarily before the competitions until the calibration is done. The calibration markers are simple blue LEDs. The pose of the camera is defined as the six parameters that describe the physical orientation of the camera. These are roll, pitch, yaw, $x$, $y$, and $z$. These parameters are visualized below.
Figure 83: Pitch and Z Pose Parameters, Side View

Figure 84: Roll Pose Parameter, View of Camera From Behind

Figure 85: Yaw, X, Y Pose Parameters Shown, Overhead View of Camera
Initially, we sought to implement a calibration algorithm that develops a guess for the camera's pose, simulates an image of markers from that pose, and minimized the error between the simulated image and an actual image by iteratively changing different parameters of the guessed pose. After this was found to be ineffective, we implemented an approach to calibration that iteratively optimized the rotation of the camera, and the location of the camera, using an object-space co-linearity error vector as defined by Lu, Hagar, and Mjolsness [11].

Our first attempt to calibrating the camera tried to assume camera locations, simulate images from those locations, and compare the simulated image to the actual image. This idea was based on the fact that we had an actual image, we had mathematics that describe how to simulate an image based on a guessed camera pose and object locations, and minimizing the differences between the actual and simulated images by changing our guessed pose would allow us to accurately determine the actual camera's location. We defined the error in an image as the sum of pixel distances between objects in the actual image and simulated image. Figure 86 below shows the individual errors between objects in one image (squares) and another image (triangles).

Figure 86: Error between Two Images
Using this error definition, we found a value for an arbitrary degree of freedom in the camera's pose that minimizes the error. We then incorporated that value into the guess for the camera pose, and proceeded to find a value that minimized the image error for a different degree of freedom, repeating until the pose stopped changing, or a maximum number of iterations was reached. This approach ran into issues because it attempted to optimize the 6 degrees of freedom of the camera individually, which caused convergence issues, and unsatisfactory results in simulation. These results motivated us to find a more established algorithm to solve this issue.

The Orthogonal Iteration Algorithm developed by Lu et al. developed a solution to the calibration problem by separating the pose into two variables, instead of six, and using an object-space error vector, rather than an image-space error vector [12]. This object space colinearity error vector is again based on the pin-hole camera model, and its idea that the focal point of the camera, the projection of an object on the image plane, and the actual image should be collinear. Thus the error vector $e_i$ is described as:

$$ e_i = (I - F_i)(R(p_i - t)) $$

(5.7)

Where $F_i = \frac{v_i^T v_i}{v_i^T v_i}$ is projection operator, and $v_i = [u, v, 1]^T$ is the image of $p_i = [x, y, z]^T$ on the camera’s image plane, and R and t are a 3x3 rotation matrix and 3x1 displacement vector respectively which describe the pose of the camera in field coordinates. Figure 87 below shows how R and t serve as a frame transformation between the object reference frame, or field coordinates, and the camera reference plane.
Using equation 5.7, R and t could be iteratively optimized. This was done by computing:

$$\sum |e_i| = \sum_{i=0}^{n} |(I - F_i)(R(p_i - t))|$$  \hspace{1cm} (5.8)

Where n is the number of calibration markers used. Then values of R and t were found to minimize the sum of the errors. This method of calibration was much more effective at determining the camera’s pose than using image space error as described in Figure 86, allowing accurate position reconstructions in both simulations and real-world tests.
Chapter 6: System Testing

With the entirety of the system implemented, we moved on to testing. The system as a whole was tested in an environment that was meant to emulate a FIRST arena. We used our single camera to take and process images from locations exactly as they would be positioned in a real FIRST environment. We placed the LED beacon so that it was visible to three typical camera locations of our system. This was done to demonstrate the ability to use stereo-vision concepts incorporating more than two cameras spaced far apart. We also performed tests using just two cameras. From each camera position, we captured an image of the arena so that it could be processed offline. We had to process the data offline because we did not have the resources available to us to replicate our hardware.

Figure 88 shows the testing equipment for viewing the LED beacon and communicating with the PC. The FPGA board and camera are held inside an acrylic case that we fashioned specifically to hold these items and support all of our testing operations. The case holding the camera and FPGA subsystem can be manually tilted and fixed to a certain pose. There is access to the lens for manual focusing, as well as access to the switches and buttons for mode control. Two USB wires connect the PC to the FPGA board for development as well as high speed serial communication.
We preliminarily performed two small scale tests with two cameras spaced ten feet apart. In these tests, two cameras were used to reconstruct the locations of beacons placed relatively close to the cameras. In the first of these, the beacon was located (in inches) at (32, 63) and was reconstructed at (32, 60) with an error of three inches. In the second test, the beacon was located at (54, 70) and was reconstructed at (54, 75) with an error of five inches.

After performing our preliminary tests and verifying that the system functioned properly, we began executing larger scale tests. In our first larger scale test, we placed the beacon at location (123, 198) and used cameras in three locations of the side of our simulated arena to locate the beacon. This test was done to confirm the ability to use more than two cameras for reconstruction of locations. The result was (118, 202) which corresponds to an error of about six inches.
After completing the first test, we performed another test by placing the beacon at (98, 166) and performing the reconstruction using two cameras placed at corners of the arena spaced 27 feet apart. The results of this test can be seen in Figure 89 below.

![Figure 89: Actual Beacon (98, 166) Compared to Reconstructed Location (106, 166) in Test 2. Total Error: 8 Inches](image)

In this test, the reconstruction algorithm found the beacon to be eight inches away from where it was actually located.

For our final test, we placed the beacon at (62, 132) and again ran the system with two cameras spaced 27 feet apart. The results of this test can be seen in Figure 90 below. In this test the reconstruction algorithm found the beacon to be two inches away from the actual beacon location.
The actual beacon locations and reconstructed beacon locations for the three larger scale tests are plotted in Figure 91 below.
After analyzing the results of the tests, we found that the maximum error was 8 inches and the minimum error was two inches. We believe the range of these results to be due to the fact that the rig used to hold the camera in place was not entirely stable and the lens of the camera required focusing between calibration and beacon images. These two factors combined to create slight errors between the location of the camera as determined by the calibration algorithm and the actual location of the camera when the reconstruction image was taken. In the FIRST environment, the cameras would be firmly locked in place, and not require manual focusing during the competition, and this source of error would be greatly diminished.
Chapter 7: Conclusions

The robot localization system we designed and implemented successfully met all of our system requirements and goals except for a slightly larger error than we were striving for. The system was carefully designed and developed with the requirements in mind, and the result was a system that is close to being able to be implemented by FIRST with a minor lens upgrade, and implementation of an FPGA-based Ethernet controller. The lens would need a larger field of view to cover the intended area, and the Ethernet controller would enable FIRST to transmit data across the entire field effectively.

The essential requirement that our system be able to detect and identify all robots separately was met. This was done by using programmable LED beacons that give twelve unique patterns for use by the robots. The beacon identification algorithms were successfully able to identify these patterns in the camera frames and associate them with the appropriate unique identifier. This was made possible by the very careful design of the embedded FPGA system. The processes that are run by the FPGA hardware as well as the soft-core Microblaze processor were extensively planned out before implementation and developed with exhaustive attention to detail in order to achieve the best possible results for identification.

Testing indicates that the coordinates generated for the beacons are consistently accurate to eight or fewer inches. While eight inches maximum error is above our ideal accuracy, it is still reasonably accurate such that it would be of use to the competitors. Additionally, small variations were present in the system due to human error. This was caused by repeatedly moving the single camera/FPGA system to multiple locations in order to simulate using multiple cameras. In a real FIRST environment, the cameras would be held steady and no manual lens
adjustment would be required during operation and therefore, the results would be slightly improved.

The requirement that our system be minimally invasive was met. One way we met this requirement was to use automated calibration to allow setup to be simple and not force the volunteers to place the cameras in an extremely precise location. Another way we met this requirement was to make an LED beacon that is small, light, and low enough in power that it can be fitted to the robots.

Low maintenance operation was achieved successfully. One way we achieved this was by adding the capability of powering the beacons using the robots’ on-board power sources to power the LED beacons. The cameras and their associated embedded systems are powered by a wall outlet, which is readily accessible at FIRST competitions. The LED beacons are durable enough for use in the competitions, as long as they are placed on the robots in the right locations so that they are not hit directly by other robots with excessive force.

The ability of the system to be robust and flexible in a competitive environment was achieved successfully. This was accomplished primarily inside the image processing embedded systems. To prevent false identifications or bottlenecking due to excessive data requirements, the embedded systems filter and normalize the incoming frames specifically to preserve the beacons and as little background noise as possible. System testing was done inside Harrington Auditorium as well as inside the MQP lab in different lighting conditions and operation was consistently smooth.

7.1: Future Work

Testing thus far has been performed by using our single-camera rig to capture images from multiple locations in order to simulate the effect of having multiple cameras by taking
instantaneous snapshots of the test environment. However, the single-camera rigs are all identical to one another. This means that implementing a full real-time system is possible by simply replicating our hardware with a minor lens upgrade. Supporting the networking of all six cameras with the PC over Ethernet would allow FIRST to save money.

The lens available for us during testing did not have the desired field of view or depth of field. In order to make the full system capable of seeing the entire field, a new lens with the proper field of view is desired. No modifications to the rest of the hardware would be required to use a new lens, and only the two lens angle parameters inside the PC source code would need to be edited.

The range of our tests was limited by the visibility of the beacon. As the beacon was farther away in the images, the color differences within the LED matrix became obscured. This meant that the beacon did not appear to have discrete colored sections to the camera, and this compromised our algorithms. However, a simple and practical solution to this problem would be to use four LED matrices instead of one. These would be placed in a square pattern, and one entire LED matrix would be one color, and the other three would be another color. This would make the smallest quadrant of the matrix four times larger than it is currently, and it would be seen far more consistently at range. The total beacon size would be six by six inches after the revision.
References


Appendix A: Beacon Control Code

The source code below was used to control the patterns displayed on the LED matrix.

This system allowed us to generate unique patterns for each robot which allows multiple robots
to be tracked simultaneously.

```c
#include <msp430g2553.h>
#include <stdio.h>
#include <string.h>
#define row1 BIT0
#define row2 BIT1
#define red1 BIT2
#define red2 BIT3
#define green1 BIT4
#define green2 BIT5
#define blue1 BIT7
#define blue2 BIT6
#define Button BIT3

static int ButtonCount = 0;
static int ulButtons;
static int lastButton = 0;
static int top_bot_actual = 0;
static int top_bot = 0;
static int counter = 0;

void main(void) {
    WDTCTL = WDTPW + WDTHOLD;
    //reset watch dog timer
    TA0CCCTL0 = CCIE;
    //Timer A0 setup
    TA0CTL = TASSEL_2 + MC_1 + ID_3;
    TA0CCR0 = 12000;
    TA1CCCTL0 = CCIE;
    //Timer A1 setup
    TA1CTL = TASSEL_2 + MC_1 + ID_0;
    TA1CCR0 = 124;
    _BIS_SR(GIE);
    P2SEL &= ~BIT6;
    //selecting general I/O
    P2SEL &= ~BIT7;
    //selecting general I/O
    P2OUT = 0;
    //setting outputs to 0
```
P2DIR |= row1 + row2 + red1 + red2 + green1 + green2 + blue1 + blue2;
//setting pins to output

P1REN = BIT3;
P1SEL = 0;
P1DIR &= ~BIT3;
P1IN |= BIT3;//read from P1IN port 3 to find out if button's pressed
}

// Timer A0 interrupt service routine
#pragma vector=TIMER0_A0_VECTOR
__interrupt void Timer0_A (void)
{
    ulButtons = ((P1IN & Button) != Button);

    if((lastButton == 0) && ulButtons)
        if(ButtonCount + 1 > 13) // Count up 13 for button press to
            change between beacon patterns.
            ButtonCount = 0;
        else
            ButtonCount++;

    lastButton = ulButtons;
}

#pragma vector=TIMER1_A0_VECTOR
__interrupt void Timer1_A (void)
{
    if(counter > 31)
        counter = 0;
    else
        counter++;

    if(top_bot_actual == 0) //Switches between top set of rows
        and bottom set in order to multiplex
        top_bot_actual = 1;
    else
        top_bot_actual = 0;

    if(counter >= 10) // 12 default
        top_bot = 2;
    else
        top_bot = top_bot_actual;

    switch(ButtonCount)
    {
    case 0:
        P2OUT &= row1 + row2;
        //Set
        Matrix output to be off when powered.
        break;
case 1:
  if (top_bot == 0) {
    P2OUT &= row2;
    P2OUT |= (((~row1 & red1) + row2) | ((~row1 & red2) + row2));
    // Set matrix top row to display red in top left
    // and red in top right
  } else if (top_bot == 1) {
    P2OUT &= row1;
    P2OUT |= (((~row2 & red1) + row1) | ((~row2 & red2 + blue2) + row1));
    // Set matrix bottom row to display red in lower left
    // and purple in lower right
  } else
    P2OUT &= row1 + row2;
  break;

case 2:
  if (top_bot == 0) {
    P2OUT &= row2;
    P2OUT |= (((~row1 & red1) + row2) | (~row1 & red2 + row2));
    // Set matrix top row to display red in top left
    // and red in top right
  } else if (top_bot == 1) {
    P2OUT &= row1;
    P2OUT |= (((~row2 & red1) + row1) | (~row2 & red2 + green2) + row1));
    // Set matrix bottom row to display red in lower left
    // and yellow in lower right
  } else
    P2OUT &= row1 + row2;
  break;

case 3:
  if (top_bot == 0) {
    P2OUT &= row2;
    P2OUT |= (((~row1 & red1) + row2) | (~row1 & red2 + row2));
    // Set matrix top row to display red in top left
    // and red in top right
  } else if (top_bot == 1) {
    P2OUT &= row1;
P2OUT |= (((~row2 & red1) + row1) | ((~row2 & green2) + row1));  //Set matrix bottom row to display red in lower left

//and green in lower right
else
  P2OUT &= row1 + row2;
break;

case 4:
  if(top_bot == 0){
    P2OUT &= row2;
    P2OUT |= (((~row1 & green1 + red1) + row2) | ((~row1 & green2 + red2) + row2));  //Set matrix top row to display yellow in top left

    //and yellow in top right
    } else if(top_bot == 1){
      P2OUT &= row1;
      P2OUT |= (((~row2 & green1 + red1) + row1) | ((~row2 & green2 + red2) + row1));  //Set matrix bottom row to display yellow in lower left

    //and red in lower right
    } else
      P2OUT &= row1 + row2;
break;

case 5:
  if(top_bot == 0){
    P2OUT &= row2;
    P2OUT |= (((~row1 & green1 + red1) + row2) | ((~row1 & green2 + red2) + row2));  //Set matrix top row to display yellow in top left

    //and yellow in top right
    } else if(top_bot == 1){
      P2OUT &= row1;
      P2OUT |= (((~row2 & green1 + red1) + row1) | (row2));  //Set matrix bottom row to display yellow in lower left

    //and green in lower right
    } else
      P2OUT &= row1 + row2;
break;

case 6:
  if(top_bot == 0){
    P2OUT &= row2;
P2OUT |= (((~row1 & green1 + red1) + row2) | ((~row1 & green2 + red2) + row2)); //Set matrix top row to display yellow in top left

//and yellow in top right
else if (top_bot == 1) {
P2OUT &= row1;
P2OUT |= (((~row2 & green1 + red1) + row1) | ((~row2 & red2 + blue2) + row1)); //Set matrix bottom row to display yellow in lower left

//and purple in lower right
} else
P2OUT &= row1 + row2;
break;

case 7:
if (top_bot == 0) {
P2OUT &= row2;
P2OUT |= (((~row1 & green1) + row2) | ((~row1 & green2) + row2)); //Set matrix top row to display green in top left

//and green in top right
} else if (top_bot == 1) {
P2OUT &= row1;
P2OUT |= (((~row2 & green1) + row1) | ((~row2 & red2) + row1)); //Set matrix bottom row to display green in lower left

//and red in lower right
} else
P2OUT &= row1 + row2;
break;

case 8:
if (top_bot == 0) {
P2OUT &= row2;
P2OUT |= (((~row1 & green1) + row2) | ((~row1 & green2) + row2)); //Set matrix top row to display green in top left

//and green in top right
} else if (top_bot == 1) {
P2OUT &= row1;
P2OUT |= (((~row2 & green1) + row1) | ((~row2 & red2 + green2) + row1)); //Set matrix bottom row to display green in lower left
//and yellow in lower right
} else
    P2OUT &= row1 + row2;
break;

case 9:
    if (top_bot == 0) {
        P2OUT &= row2;
P2OUT |= (((~row1 & green1) + row2) | ((~row1 & green2) + row2));
        //Set matrix top row to display green in top left
    } else if (top_bot == 1) {
        P2OUT &= row1;
P2OUT |= (((~row2 & green1) + row1) | ((~row2 & red2 + blue2) + row2));
        //Set matrix bottom row to display green in lower left
    } else
        P2OUT &= row1 + row2;
break;

case 10:
    if (top_bot == 0) {
        P2OUT &= row2;
P2OUT |= (((~row1 & blue1 + red1) + row2) | ((~row1 & blue2 + red2) + row2));
        //Set matrix top row to display purple in top left
    } else if (top_bot == 1) {
        P2OUT &= row1;
P2OUT |= (((~row2 & blue1 + red1) + row1) | ((~row2 & red2) + row1));
        //Set matrix bottom row to display purple in lower left
    } else
        P2OUT &= row1 + row2;
break;

case 11:
    if (top_bot == 0) {
        P2OUT &= row2;
    } else if (top_bot == 1) {
        P2OUT &= row1;
P2OUT |= (((~row2 & blue1 + red1) + row1) | ((~row2 & red2) + row1));
        //Set matrix bottom row to display purple in lower left
    } else
        P2OUT &= row1 + row2;
break;
```c
P2OUT |= (((~row1 & blue1 + red1) + row2) | ((~row1 & blue2 + red2) + row2)); //Set matrix top row to display purple in top left

//and purple in top right
} 
else if(top_bot == 1){
P2OUT &= row1;
P2OUT |= (((~row2 & blue1 + red1) + row1) | ((~row2 & green2 + red2) + row1)); //Set matrix bottom row to display purple in lower left

//and yellow in lower right
} 
else
P2OUT &= row1 + row2;
break;

case 12:
if(top_bot == 0){
P2OUT &= row2;
P2OUT |= (((~row1 & blue1 + red1) + row2) | ((~row1 & blue2 + red2) + row2)); //Set matrix top row to display purple in top left

//and purple in top right
} 
else if(top_bot == 1){
P2OUT &= row1;
P2OUT |= (((~row2 & blue1 + red1) + row1) | ((~row2 & green2) + row1)); //Set matrix bottom row to display purple in lower left

//and green in lower right
} 
else
P2OUT &= row1 + row2;
break;
```
Appendix B: LED Matrix Controller Schematic

The following schematic shows the connections required to implement the LED Matrix Controller. The PCB generated from this schematic was used with the Beacon Control Code in Appendix A to generate the unique patterns used to identify multiple robots simultaneously.
Appendix C: Verilog Modules

The Verilog code below is the top level module that was implemented for the Image Acquisition and Image Processing stages. These stages were used to interface with the camera, store frames, and process the images for each camera. This is only a small subsection of the Verilog design in order to keep the size of this report manageable. The full source code for this design is available if requested. The names of the other Verilog Modules used in this system are: Camera_In, Processing, RAM_Interface, and VGA_Display.

`timescale 1ns / 1ps
// This module is the top level module for the Image Acquisition and Image Processing stages of the system. In this module, data is taken from the camera in YUV format, converted to RGB format and stored in RAM. After a frame has been stored in RAM, the Microblaze begins processing the image to determine the center of each beacon and which pattern it is displaying. Once this is complete, the data is sent via UART communications to a Central PC for processing.
module top_level(
    input FPGA_clk,
    input reset,
    input next_frame,
    input dclk,
    input HREF,
    input VREF,
    input filter,
    input auto_mode,
    input UART_Rx,
    input [2:0] switch,
    input [7:0] din,
    output adv_l,
    output lb_l,
    output ub_l,
    output ce_l,
    output oe_l,
    output we_l,
    output cre_l,
    output flash_ce,
    output clk_RAM,
    output HS,
    output VS,
    output UART_Tx,
    output [7:0] VGA_Color,
    output [7:0] led,
    output [22:0] addr,
    inout [15:0] dq
);
// Horizontal Pixel Resolution
parameter HPIXELS = 640;
// Vertical Pixel Resolution
parameter VPIXELS = 480;
// Total number of pixels in frame based on HPIXELS and VPIXELS
parameter NUM_PIXELS = HPIXELS*VPIXELS;

// Values assigned to state labels
parameter [2:0] WAIT_STATE = 0, CAMERA_DATA = 1, FINAL_DATA = 2,
MICROBLAZE = 3, VGA_DISPLAY = 4;

wire ready;
wire valid_camera_data;
wire valid_processed_data;
wire clk_80M;
wire processing_complete;
wire display;
wire data_valid;
wire VGA_FIFO_Full;
wire FIFO_reset;
wire powering_up;
wire clk_25M_180;
wire clk_54M;
wire clk_25M;
wire ready_2;
wire auto_next_frame;
wire microblaze_active;
wire blob_next_frame;
wire blob_read;
wire [31:0] camera_data;
wire [63:0] processed_data;
wire [63:0] RAM_dout;
wire [6:0] led_outputs;
wire [31:0] GPI1, GPI2, GPI3;
wire [31:0] GPO1;

reg last_ready;
reg last_VREF;
reg last_read;
reg [2:0] last_state;
reg [2:0] current_state, next_state;
reg [11:0] HLimit;
reg [22:0] addr_in;
reg [24:0] timer;

// clk_converter takes in 100 MHz clock input and creates other clock
signals.
clk_converter inst_clk_converter ( 
.CLK_IN1(FPGA_clk), // In - 100 MHz clock
.clk_100M(clk_100M), // Out - 100 MHz clock
.clk_80M(clk_80M), // Out - 80 MHz clock
.clk_25M(clk_25M), // Out - 25 MHz clock
.clk_25M_180(clk_25M_180) // Out - 25 MHz clock 180 degree phase
)

// Camera_In receives data from the camera and packages macropixels together
Camera_In inst_Camera_In(
    .clk(dclk), // In - 54 MHz clock
    .reset(FIFO_reset), // In - Reset
    .read(Camera_In_read), // In - FIFO read signal
    .write(Camera_In_write), // In - FIFO write signal
    .din(din), // Out - Image data [7:0]
    .valid(valid_camera_data), // Out - FIFO valid
    .dout(camera_data) // Out - Macropixel of data [31:0]
);

// Processing module converts from YUV to RGB and applies filters
Processing inst_Processing(
    .clk(clk_80M), // In - 80 MHz clock
    .valid_in(valid_camera_data), // In - Valid data
    .filter(filter), // In - Activate Filtering
    .reset(FIFO_reset), // In - Reset
    .ready(ready_2), // In - FIFO read control. RAM ready for data
    .camera_data(camera_data), // In - Image Data [23:0]
    .valid_out(valid_processed_data), // Out - Valid data on output
    .processed_data_out(processed_data), // Out - Processed data [63:0]
    .processing_complete(processing_complete) // Out - Processing has finished
);

// Performs RAM reads and writes
RAM_Interface inst_RAM_interface(
    .din(processed_data), // In - Din [63:0]
    .read(RAM_read), // In - Read command
    .write(RAM_write), // In - Write command
    .clk(clk_80M), // In - 80 MHz clock
    .reset(reset), // In - Reset
    .addr_in(addr_in), // In - Address [22:0]
    .clk_out(clk_RAM), // Out - 80 MHz clock
    .adv_l(adv_l), // Out - Adv
    .lb_l(lb_l), // Out - LB
    .ub_l(ub_l), // Out - UB
    .ce_l(ce_l), // Out - CE
    .oe_l(oe_l), // Out - OE
    .we_l(we_l), // Out - WE
    .cre_l(cre_l), // Out - CRE
    .flash_ce(flash_ce), // Out - Flash CE
    .ready(ready), // Out - Ready for operation
    .dout_valid(data_valid), // Out - Output data valid
    .powering_up(powering_up), // Out - RAM is in powering up state
    .addr_out(addr), // Out - Address to RAM
    .dout(RAM_dout), // Out - Dout [63:0]
    .dq(dq) // InOut - RAM data line [15:0]
);

// Microblaze soft-core processor
MCS mcs_0 (
    .Clk(clk_100M), // IN - 100 MHz clock
    .Reset(reset), // In - Reset
    .UART_Rx(UART_Rx), // In - UART_Rx
    .UART_Tx(UART_Tx), // Out - UART_Tx
    .GPO1(GPO1), // Out - [31 : 0] GPO1
.GPI1(GPI1),              // In - [31 : 0] GPI1
    GPI1 Interrupt(),   // Out - GPI1 Interrupt
.GPI2(GPI2),            // In - [31 : 0] GPI2
    GPI2 Interrupt(),   // Out - GPI2 Interrupt
.GPI3(GPI3),            // In - [31 : 0] GPI3
    GPI3 Interrupt()    // Out - GPI3 Interrupt
);

// VGA control module
VGA_Display inst_VGA_Display(
    .reset(reset),        // In - Reset
    .VGA_clk(clk_25M),    // In - 25 MHz clock
    .clk_25M_180(clk_25M_180), // In - 180 degree out of phase 25 MHz clock
    .clk_80M(clk_80M),   // In - 80 MHz clock
    .display(display),   // In - Display active
    .data_valid(data_valid), // In - RAM data valid
    .data(RAM_dout),     // In - RAM data [63:0]
    .VGA_FIFO_Full(VGA_FIFO_Full), // Out - FIFO full
    .HS(HS),            // Out - Horizontal Sync
    .VS(VS),            // Out - Vertical Sync
    .VGA_Color(VGA_Color) // Out - Pixel color [7:0]
);

// Limit number of pixels per line to HPIXELS
always @(posedge dclk)
    begin
        if(~HREF)
            HLimit <= 0;
        else
            HLimit <= HLimit + 1'b1;
    end

// Pulse detection for microblaze RAM read
always @(posedge clk_80M)
    last_read <= blob_read;

// Increment addr
always @(posedge clk_80M)
    begin
        last_ready <= ready;

        if((last_state == FINAL_DATA && current_state == MICROBLAZE) ||
           (last_state == MICROBLAZE && current_state == VGA_DISPLAY) ||
           (current_state == VGA_DISPLAY && ~VS))
            addr_in <= 0;
        else if(current_state != WAIT_STATE)
            begin
                if(~ready && last_ready)
                    begin
                        if(addr_in + 3'h4 < NUM_PIXELS/2-1)
                            addr_in <= addr_in + 3'h4;
                        else
                            addr_in <= 0;
                    end
            end
        else
            addr_in <= 0;
    end
// Process/transmit state machine
always @(posedge clk_80M)
    if(reset)
        current_state <= WAIT_STATE;
    else
        current_state <= next_state;

// Next state logic
always @(current_state, VREF, processing_complete, last_VREF, next_frame,
    powering_up, addr_in, blob_next_frame, auto_next_frame)
    case(current_state)
        WAIT_STATE:
            if(powering_up || next_frame)
                next_state <= WAIT_STATE;
            else if(last_VREF && ~VREF)
                next_state <= CAMERA_DATA;
            else
                next_state <= WAIT_STATE;
        CAMERA_DATA:
            if(powering_up || next_frame)
                next_state <= WAIT_STATE;
            else if(~last_VREF && VREF)
                next_state <= FINAL_DATA;
            else
                next_state <= CAMERA_DATA;
        FINAL_DATA:
            if(powering_up || next_frame)
                next_state <= WAIT_STATE;
            else if(processing_complete)
                next_state <= MICROBLAZE;
            else
                next_state <= FINAL_DATA;
        MICROBLAZE:
            if(powering_up || next_frame)
                next_state <= WAIT_STATE;
            else if(blob_next_frame)
                next_state <= VGA_DISPLAY;
            else
                next_state <= MICROBLAZE;
        VGA_DISPLAY:
            if(powering_up || next_frame || auto_next_frame)
                next_state <= WAIT_STATE;
            else
                next_state <= VGA_DISPLAY;
        default:
            next_state <= WAIT_STATE;
    endcase

// Delay VREF
always @(posedge clk_80M)
begin
    last_VREF <= VREF;
    last_state <= current_state;
end

// Display image for 1 second
always @(posedge clk_25M)
    if(current_state != VGA_DISPLAY || timer >= 25000000)
        timer <= 0;
    else
        timer <= timer + 1'b1;

// Control signals for Camera_In FIFO
assign Camera_In_read = (current_state == CAMERA_DATA || current_state == FINAL_DATA || current_state == WAIT_STATE);
assign Camera_In_write = (HREF && current_state == CAMERA_DATA && (HLimit <= ((HPIXELS*2)-1)));

// RAM read/write control signals
assign RAM_write = valid_processed_data && (current_state != VGA_DISPLAY && !microblaze_active);
assign RAM_read = (microblaze_active) ? ~last_read && blob_read :
    (current_state == VGA_DISPLAY && ~VGA_FIFO_Full);

// Activate VGA Display
assign display = (current_state == VGA_DISPLAY);

// Provide Reset signal to FIFOs
assign FIFO_reset = reset | next_frame | auto_next_frame;

// Provide ready signal to Converting Module to ensure empty FIFOs
assign ready_2 = ready | (current_state == WAIT_STATE);

// Wait set amount of time, then initiate new frame grab
assign auto_next_frame = (timer == 5000000) && auto_mode;

// Microblaze given control of RAM
assign microblaze_active = (current_state == MICROBLAZE);

// Microblaze RAM Inputs
assign GPI1 = RAM_dout[63:32];
assign GPI2 = RAM_dout[31:0];

// Microblaze Control Inputs
assign GPI3 = {data_valid, microblaze_active, (ready && ~powering_up),
    switch, 26'b0};

// Microblaze Control Outputs
assign blob_next_frame = GPO1[31];
assign blob_read = GPO1[30];
assign led_outputs = GPO1[29:23];
endmodule
Appendix D: Section of Image Processing Code

The source code seen below is the main function of the Image Processing stage. This stage was used to search through a frame worth of filtered image data and determine the location and patterns associated with all beacons that were visible to the camera. This is only a small subsection of the Image Processing Code in order to keep the size of this report manageable. The full source code for this design is available if requested.

```c
int main() {
    unsigned int v, x;
    unsigned int Neighbor, transmit;
    int Current_MaxMarker;
    int Current Marker;
    init_platform();

    // Initialize GPO and GPI
    SRAM63_32 = XIOModule_Initialize(&gpi1, XPAR_IOMODULE_0_DEVICE_ID);
    SRAM63_32 = XIOModule_Start(&gpi1);
    SRAM31_0 = XIOModule_Initialize(&gpi2, XPAR_IOMODULE_0_DEVICE_ID);
    SRAM31_0 = XIOModule_Start(&gpi2);
    incontrols = XIOModule_Initialize(&gpi3, XPAR_IOMODULE_0_DEVICE_ID);
    incontrols = XIOModule_Start(&gpi3);
    outcontrols = XIOModule_Initialize(&gpo1, XPAR_IOMODULE_0DEVICE_ID);
    outcontrols = XIOModule_Start(&gpo1);

    // Determine number of pixels between patches in order to merge
    val = roundDivide(hpixels, 200);

    // Loop while system is powered
    while(1){
        overflow = 0;
        numBeacons = 0;

        // Wait for FPGA to signal that an image is ready to be processed
        while(transmit == 0){
            transmit = (XIOModule_DiscreteRead(&gpi3, 3) << 1) >> 31;
        }

        // Reset MaxMarker for each frame
        MaxMarker = 0;

        // Search the frame for all patches of color
        for(v = 0; v < vpixels && !overflow; v++)
            Current Marker = 0;
        Current_MaxMarker = 0;

        // Acquire a new line of pixels
        GetNewPixels();

        // Scan a line of pixels for color
```
for(x = 0; x < hpixels-1 && !overflow; x++){
    // Check Pixel
    if(pixelarray[x] != 0) {
        if(x == 0) {
            // Pixel has no color
            Neighbor = 0;
        } else {
            // Pixel has neighboring pixels with color
        }
    } else {
        // Pixel has no neighboring pixels with color
        Neighbor = 2;
    }

    // Determine which patch the pixel belongs to
    if(Neighbor == 0){
        if((Current_MaxMarker + 1) <= max_blobs){
            Current_Marker = Current_MaxMarker;
            Current_MaxMarker++;
        } else {
            Current_Marker = Current_MaxMarker;
            overflow = 1;
            break;
        }
        // Create new run
        Current_Run[start_pixel][Current_Marker] = x;
        Current_Run[end_pixel][Current_Marker] = x;
        Current_Run[current_color][Current_Marker] = pixelarray[x];
    } else if(Neighbor == 1){
        // Add pixel to current run
        Current_Run[end_pixel][Current_Marker] = x;
    }
    if(Current_MaxMarker != 0){
        // Add pixel to marker
        UpdateMarker(Current_MaxMarker, v);
    }
}
// Request new frame (set next_frame up to high and then low again)
outcontrols |= 0x80000000;
XlOModule_DiscWrite(&gpol, 1, outcontrols);

// Scan through all patches and merge patches that are adjacent
Merge();
// Identify all beacons within the frame and match a pattern to the beacons
Identify();
// After all beacons have been identified, transmit data via UART to central PC
Transmit();

// Clear all data after transmission is complete to prevent issues with the next frame
for (v = 0; v < max_blobs; v++)
{
    for (x = 0; x < 10; x++)
    {
        if (x < 3)
            Current_Run[x][v] = 0;
        Run[x][v] = 0;
    }
}

// Signal FPGA that image processing is complete
outcontrols &= 0x7FFFFFFF;
XIONModule_DiscreteWrite(&gpo1, 1, outcontrols);

cleanup_platform();
return 0;
Appendix E: Sample of Processing Code

This Application implements the image model described in Chapter 4.3, to simulate camera images of objects. It requires other classes implemented for this system, such as Field and CameraSettings to function. These libraries are available upon request.

```java
int currentView = 1;
int nextView = 1;
Field pField;

void setup()
{
    setupFieldSimulation();
}

void draw()
{
    if (currentView!=nextView)
    {
        currentView = nextView;
        fill(color(255));
        rect(0, 0, width, height);
        drawGrid();
        CameraImage frame2 = pField.generateCameraImage(currentView);
        frame2.generatePositionsFromImage();
    }
}

void mousePressed()
{
    nextView++;
    nextView = nextView>pField.cameras.size()? 1:nextView;
}

void drawGrid()
{
    fill(color(0));
    for (int i=0; i< width; i+=40)
    {
        int strokeWidth = i%200 ==0? 2:1;
        strokeWeight(strokeWidth);
        line(i, 0, i, height);
        text(i,i,10);
    }
    for (int j=0; j<height; j+=40)
    {
        int strokeWidth = j%200 ==0? 2:1;
```
void setupFieldSimulation()
{
  size(1280, 1024);
  background(color(255));
  stroke(color(0));
  rect(0, 0, width, height);

  pField = new Field();
  drawGrid();
  Beacon beacon1 = new Beacon(30, 30, -60, color(0, 0, 255));
  Beacon beacon2 = new Beacon(50, 30, -60, color(0, 0, 255));
  Beacon beacon3 = new Beacon(35, 50, -60, color(0, 0, 255));
  Beacon beacon4 = new Beacon(18, 20, -60, color(0, 0, 255));
  Beacon beacon5 = new Beacon(35, 10, -60, color(0, 0, 255));
  Beacon beacon6 = new Beacon(18, 40, -60, color(0, 0, 255));

  pField.addBeacon(beacon1);
  pField.addBeacon(beacon2);
  pField.addBeacon(beacon3);
  pField.addBeacon(beacon4);
  pField.addBeacon(beacon5);
  pField.addBeacon(beacon6);

  CameraSettings cam1 = new CameraSettings(0, 0, 45);
  CameraSettings cam2 = new CameraSettings(0, 60, 135);

  pField.addCamera(cam1);
  pField.addCamera(cam2);

  CameraImage frame2 = pField.generateCameraImage(currentView);
  frame2.generatePositionsFromImage();
}
Appendix F: List of Materials

This appendix shows the materials we used to implement this system and their individual costs. These parts were used in every stage of the project and were all used in the final design.

<table>
<thead>
<tr>
<th>Part</th>
<th>Manufacturer</th>
<th>Model</th>
<th>Unit cost</th>
<th>No.</th>
<th>Cost (full system)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Camera</td>
<td>Videology</td>
<td>24CL35D1G</td>
<td>$207.11</td>
<td>1</td>
<td>$207.11</td>
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<tr>
<td>Lens</td>
<td>Videology</td>
<td>32S2920N</td>
<td>$20.50</td>
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<td>FPGA Board</td>
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<td>Nexys3</td>
<td>$130.00</td>
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<tr>
<td>Custom Camera Breakout PCB</td>
<td>Advanced Circuits</td>
<td>custom</td>
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<tr>
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<td>Futurlec</td>
<td>LEDMB8RGBC5 LED Dot Matrix</td>
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<tr>
<td>LED microcontroller board</td>
<td>Texas Instruments</td>
<td>MSP430 Launchpad</td>
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<td>1</td>
<td>$5.00</td>
</tr>
</tbody>
</table>

Total cost: $466.51